# The Statistical Sleuth in R: Chapter 6

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#### Introduction 1

This document is intended to help describe how to undertake analyses introduced as examples in the Second Edition of the *Statistical Sleuth* (2002) by Fred Ramsey and Dan Schafer. More information about the book can be found at http://www.proaxis.com/~panorama/home.htm. This file as well as the associated knitr reproducible analysis source file can be found at http://www.amherst. edu/~nhorton/sleuth.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web. org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignette (http://cran.r-project. org/web/packages/mosaic/vignettes/MinimalR.pdf).

To use a package within R, it must be installed (one time), and loaded (each session). The package can be installed using the following command:

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## 2 DISCRIMINATION AGAINST THE HANDICAPPED

```
> install.packages('mosaic')  # note the quotation marks
```

Once this is installed, it can be loaded by running the command:

> require(mosaic)

This needs to be done once per session.

In addition the data files for the *Sleuth* case studies can be accessed by installing the *Sleuth2* package.

```
> install.packages('Sleuth2')
```

*# note the quotation marks* 

> require(Sleuth2)

We also set some options to improve legibility of graphs and output.

```
> trellis.par.set(theme=col.mosaic()) # get a better color scheme for lattice
> options(digits=3)
```

The specific goal of this document is to demonstrate how to calculate the quantities described in Chapter 6: Linear Combinations and Multiple Comparisons of Means using R.

# 2 Discrimination Against the Handicapped

Do equivalent candidates with the same qualifications but different disabilities get treated differentially? This is the question addressed in case study 6.1 in the *Sleuth*.

# 2.1 Summary statistics and graphical display

We begin by reading the data and summarizing the variables.

```
> case0601$Handicap = relevel(case0601$Handicap, ref="Amputee")
> summary(case0601)
                     Handicap
    Score
 Min. :1.40
               Amputee
                        :14
 1st Qu.:3.70
               None
                         :14
 Median :5.05
               Crutches :14
Mean :4.93
               Hearing :14
 3rd Qu.:6.10
               Wheelchair:14
Max.
       :8.50
> favstats(Score ~ Handicap, data=case0601)
```

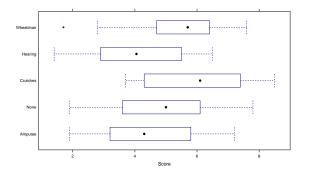
	Handicap	min	Q1	median	Q3	$\max$	mean	sd	n	missing	
1	Amputee	1.9	3.30	4.30	5.73	7.2	4.43	1.59	14	0	
2	None	1.9	3.72	5.00	6.05	7.8	4.90	1.79	14	0	
3	Crutches	3.7	4.50	6.10	7.15	8.5	5.92	1.48	14	0	
4	Hearing	1.4	3.03	4.05	5.30	6.5	4.05	1.53	14	0	
5	Wheelchair	1.7	4.72	5.70	6.35	7.6	5.34	1.75	14	0	

A total of 70 undergraduate students from a U.S. university were randomly assigned to view the tapes, 14 to each tape. The five kinds of tapes are: *None*, *Amputee*, *Crutches*, *Hearing* and *Wheelchair*. After reviewing the tape, each subject rated the qualifications of the application on 0-10 scale. Among the five handicap conditions, the *Crutches* group gave the highest mean score, while the *Hearing* group gave the lowest mean score. This is summarized on page 150 and in Display 6.1 of the *Sleuth*.

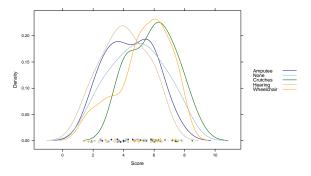
```
> with(subset(case0601, Handicap=="None"), stem(Score, scale=2))
 The decimal point is at the |
  1 | 9
  2 | 5
  3 | 06
  4 | 129
  5 | 149
  6 | 17
 7 | 48
> with(subset(case0601, Handicap=="Amputee"), stem(Score, scale=2))
 The decimal point is at the |
  1 | 9
  2 | 56
  3 | 268
 4 | 06
  5 | 3589
  6 | 1
 7 | 2
> with(subset(case0601, Handicap=="Crutches"), stem(Score, scale=1))
 The decimal point is at the |
 3 | 7
```

```
4 | 033
 5 | 18
 6 | 0234
 7 | 445
 8 | 5
> with(subset(case0601, Handicap=="Hearing"), stem(Score, scale=2))
 The decimal point is at the |
 1 | 4
  2 | 149
 3 | 479
 4 | 237
 5 | 589
 6 | 5
> with(subset(case0601, Handicap=="Wheelchair"), stem(Score, scale=2))
 The decimal point is at the |
 1 | 7
 2 | 8
 3 | 5
 4 | 78
 5 | 03
 6 | 1124
7 | 246
```

> bwplot(Handicap ~ Score, data=case0601)



> densityplot(~ Score, groups=Handicap, auto.key=TRUE, data=case0601)



The stem plots show the applicant qualification scores given by objectives. The boxplots and the density plots show that all the distributions are approximately normally distributed.

# 2.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, using all of the groups. This corresponds to the interpretations on page 151.

> anova(lm(Score ~ Handicap, data=case0601))
Analysis of Variance Table
Response: Score
 Df Sum Sq Mean Sq F value Pr(>F)
Handicap 4 30.5 7.63 2.86 0.03
Residuals 65 173.3 2.67

The p-value of p = 0.03 provides some evidence that subjects rate qualifications differently according to handicap status.

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

```
> summary(lm(Score ~ Handicap, data=case0601))
Call:
lm(formula = Score ~ Handicap, data = case0601)
Residuals:
    Min   1Q Median   3Q   Max
-3.643 -1.209   0.114   1.329   2.900
Coefficients:
```

	Estimate S	td. Error	t value	Pr(> t )
(Intercept)	4.429	0.436	10.15	5e-15
HandicapNone	0.471	0.617	0.76	0.448
HandicapCrutches	1.493	0.617	2.42	0.018
HandicapHearing	-0.379	0.617	-0.61	0.542
HandicapWheelchair	0.914	0.617	1.48	0.143

Residual standard error: 1.63 on 65 degrees of freedom Multiple R-squared: 0.15,Adjusted R-squared: 0.0974 F-statistic: 2.86 on 4 and 65 DF, p-value: 0.0301

The reference group here is *Amputee*, followed by *None*, *Crutches*, *Hearing* and *Wheelchair*. Another way of viewing these results is through a model table, which displays the differences between the grand mean and the group means.

```
> model.tables(aov(Score ~ Handicap, data=case0601))
```

Tables of effects

Handicap

Handicap								
Amputee	None	Crutches	Hearing	Wheelchair				
-0.5000	-0.0286	0.9929	-0.8786	0.4143				

Or by:

```
> mean(Score ~ Handicap, data=case0601)-mean(~ Score, data=case0601)
Amputee None Crutches Hearing Wheelchair
-0.5000 -0.0286 0.9929 -0.8786 0.4143
```

# 2.3 Contrasts and linear combination

The Tukey-Kramer test is a reasonable method for these data. We can use this to verify the calculation on page 151.

```
> tuk = TukeyHSD(aov(lm(Score ~ Handicap, data=case0601)), "Handicap", ordered=TRUE, conf.leve
> tuk
Tukey multiple comparisons of means
95% family-wise confidence level
factor levels have been ordered
Fit: aov(formula = lm(Score ~ Handicap, data = case0601))
```

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	diff	lwr	upr	p adj
Amputee-Hearing	0.379	-1.353	2.11	0.972
None-Hearing	0.850	-0.882	2.58	0.644
Wheelchair-Hearing	1.293	-0.439	3.02	0.235
Crutches-Hearing	1.871	0.140	3.60	0.028
None-Amputee	0.471	-1.260	2.20	0.940
Wheelchair-Amputee	0.914	-0.817	2.65	0.578
Crutches-Amputee	1.493	-0.239	3.22	0.123
Wheelchair-None	0.443	-1.289	2.17	0.952
Crutches-None	1.021	-0.710	2.75	0.469
Crutches-Wheelchair	0.579	-1.153	2.31	0.881

There is a plot function for a TukeyHSD object, which can be displayed by running:

> plot(tuk)

Based on the Tukey-Kramer procedure, the difference is estimated to be 1.87 points higher for the *Crutches* tapes, with a 95% confidence from 0.14 to 3.6.

Next, we calculate the comparison of Amputee/Hearing to Crutches/Wheelchair.

The t-value=3.19 supports a difference between the average scores given to the Wheelchair and Crutches handicaps and the average scores given to the Amputee and Hearing handicaps.

To verify the calculations on page 155 we used the following contrast:

```
> fit.contrast(lm(Score ~ Handicap, data=case0601), "Handicap", c(-0.5, 0, 0.5, -0.5, 0.5), con
Estimate Std. Error t value Pr(>|t|)
Handicap c=( -0.5 0 0.5 -0.5 0.5 ) 1.39 0.436 3.19 0.00218
lower CI upper CI
Handicap c=( -0.5 0 0.5 -0.5 0.5 ) 0.521 2.26
attr(,"class")
[1] "fit_contrast"
```

Other multiple comparison procedures could also be implemented. The following shows the calculation on page 164.

```
> require(agricolae)
```

#### Loading required package: agricolae

```
> LSD.test(aov(lm(Score ~ Handicap, data=case0601)), "Handicap") # LSD
> HSD.test(aov(lm(Score ~ Handicap, data=case0601)), "Handicap") # Tukey-Kramer
> LSD.test(aov(lm(Score ~ Handicap, data=case0601)), "Handicap", p.adj=c("bonferroni")) # Bon
> scheffe.test(aov(lm(Score ~ Handicap, data=case0601)), "Handicap") # Scheffe
```

The "Significant Difference" in each test result is the "95% interval half-width" described in the book.

# **3** Pre-existing Preference of Fish

Was Charles Darwin right that sexual selection is driven by females? This is the question addressed in case study 6.2 in the *Sleuth*.

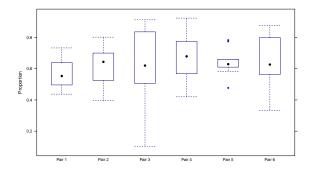
# 3.1 Summary statistics and graphical display

We begin by reading the data and summarizing the variables.

```
> summary(case0602)
  Proportion
                   Pair
                               Length
Min. :0.100 Pair 1:16
                                 :28.0
                           Min.
1st Qu.:0.531 Pair 2:14 1st Qu.:31.0
Median :0.616 Pair 3:17 Median :34.0
 Mean
       :0.621
              Pair 4:14 Mean
                                  :32.8
 3rd Qu.:0.718
              Pair 5: 9
                           3rd Qu.:34.0
Max. :0.924
              Pair 6:14
                          Max. :35.0
> favstats(Proportion ~ Pair, data=case0602)
   Pair
                 Q1 median
                             QЗ
          min
                                  max mean
                                               sd n missing
1 Pair 1 0.437 0.497 0.553 0.631 0.733 0.564 0.0902 16
                                                           0
2 Pair 2 0.396 0.531 0.644 0.696 0.802 0.609 0.1248 14
                                                           0
3 Pair 3 0.100 0.506 0.620 0.836 0.913 0.624 0.2229 17
                                                           0
4 Pair 4 0.420 0.572 0.679 0.762 0.924 0.670 0.1433 14
                                                           0
5 Pair 5 0.477 0.610 0.629 0.660 0.783 0.642 0.0941 9
                                                           0
6 Pair 6 0.334 0.568 0.627 0.789 0.876 0.633 0.1768 14
                                                           0
```

A total of 84 female fish were involved in this experiment, which is displayed on page 150.

> bwplot(Proportion ~ Pair, data=case0602)



Besides the distribution of pair 5, all distributions of other pairs are approximately normally distributed.

# 3.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, using all of the groups:

The p-value is 0.56, which doesn't provide much evidence that the mean percentage of time with the yellow-sword male differed from one male pair to another.

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

> summary(lm(Proportion ~ Pair, data=case0602)) Call: lm(formula = Proportion ~ Pair, data = case0602) Residuals: Min 1Q Median ЗQ Max -0.5243 -0.0841 0.0025 0.1086 0.2887 Coefficients: Estimate Std. Error t value Pr(>|t|) (Intercept) 0.5641 0.0386 14.60 <2e-16 PairPair 2 0.0448 0.0566 0.431 0.79

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PairPair	3	0.0602	0.0538	1.12	0.267
PairPair	4	0.1059	0.0566	1.87	0.065
PairPair	5	0.0780	0.0644	1.21	0.229
PairPair	6	0.0693	0.0566	1.22	0.224

Residual standard error: 0.155 on 78 degrees of freedom Multiple R-squared: 0.048,Adjusted R-squared: -0.0131 F-statistic: 0.786 on 5 and 78 DF, p-value: 0.563

The reference group here is pair 1, followed by pairs 2-6. Another way of viewing these results is through a model table, which displays the differences between the grand mean and the group means.

```
> model.tables(aov(Proportion ~ Pair, data=case0602))
Tables of effects
Pair
    Pair 1 Pair 2 Pair 3 Pair 4 Pair 5 Pair 6
    -0.05722 -0.01243 0.003008 0.04871 0.02083 0.01207
rep 16.00000 14.00000 14.00000 9.00000 14.00000
Or by:
> mean(Proportion ~ Pair, data=case0602)-mean(~ Proportion, data=case0602)
```

Pair 1 Pair 2 Pair 3 Pair 4 Pair 5 Pair 6 -0.05722 -0.01243 0.00301 0.04871 0.02083 0.01207

# 3.3 Contrasts and linear combination

We can calculate the values on page 152 and Display 6.5 on page 158 using contrasts.

The *t*-value is -0.46 and the one-sided *p*-value is 0.32.

```
> mean(mean(Proportion ~ Pair, data=case0602))
[1] 0.624
> t.test(mean(Proportion ~ Pair, data=case0602))
One Sample t-test
data: mean(Proportion ~ Pair, data = case0602)
t = 43, df = 5, p-value = 1e-07
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
    0.586 0.661
sample estimates:
mean of x
    0.624
```

The estimated mean percentage of time spent with the yellow-sword male is 62.4%. The one-sided *p*-value < 0.0001, and the 95% confidence interval is (58.6%, 66.1%).