

exactLoglinTest: A Program for Monte Carlo Conditional Analysis of Log-linear Models

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Nuisance parameters are parameters that are not of direct interest to the inferential question in hand. In a frequentist or likelihood paradigm, a common tool for eliminating nuisance parameters is to condition on their sufficient statistics. The same technique is useful (though rarely used) in a Bayesian settings, as it eliminates the need to put priors on nuisance parameters.

For log-linear models, conditional analysis suffers from two main drawbacks.

1. The set of lattice points contained in the conditional distribution is difficult to manage, computationally or analytically.
2. The sufficient statistics for the nuisance parameters are not ancillary to the parameters of interest.

In this manuscript we address only the first drawback using `exactLoglinTest`.

1 The Problem

The observed data, $y = (y_1, \dots, y_n)$, are modeled as Poisson counts with a means, $\mu = (\mu_1, \dots, \mu_n)$, satisfying

$$\log \mu = x\beta$$

under the null hypothesis. Here x is a full rank $n \times p$ design matrix. It is easily shown that the sufficient statistics for β under the null hypothesis are $x^t y$, where a superscript t denotes a transpose. Let h be a test statistic of interest where larger values of h support the alternative hypothesis. Two examples are the Pearson Chi-Squared statistic and the deviance. An exact test relative to h can be performed via the conditional P-value

$$\text{Prob}\{h(y) \geq h(y_{obs}) | x^t y = x^t y_{obs}\} = \sum_{\{y \in \Gamma\}} \frac{I\{h(y) \geq h(y_{obs})\}}{C \prod y_i!}$$

where y_{obs} is the observed table, C is a normalizing constant and $\Gamma = \{y | x^t y = x^t y_{obs}\}$ (often referred to as the reference set).

The term “exact” is used to refer to tests that guarantee the nominal type I error rate unconditionally. Thus a test that never rejects the null hypothesis is technically exact in any situation. Therefore, exactness is not in itself a sufficient condition for a test to be acceptable. Moreover, this example (never rejecting) is particularly relevant in our setting because Γ may contain one or few elements. Hence the conditional P-value will be exactly or near one regardless of the evidence in the data vis-a-vis the two hypotheses. However, it is also the case that the conservative conditional tests can produce P-values that are smaller than those calculated via Chi-squared approximations (see Subsection 3.2 for an example).

1.1 Binomial Calculations

Conditional inference for Poisson log-linear models contains conditional inference for binomial-logit models as a special case. Consider a binomial logit models of the form, $b_i \sim \text{Bin}(n_i, p_i)$ for $i = 1, \dots, k$ and

$$\text{logit}(p_i) = z_i \gamma + x'_i \beta, \tag{1}$$

where γ is a scalar and β is a p dimensional vector. Frequently, x'_i contains only a strata indicator and an intercept term. In this case conditioning on the sufficient statistic for β results in standard conditional

logistic regression. For this purpose, we suggest the `coxph` function as described in [7]. Instead we consider the more general case where β is arbitrary vector of nuisance parameters. However, the reader should again be warned that the loss of information from conditioning can sometimes be quite severe in these problems and hence produce useless results.

Consider testing $H_0\gamma = 0$ versus some alternative. The following model model is equivalent to the null model for (1):

$$y_{ij} \sim \text{Poisson}(\mu_{ij}) \quad \log(\mu_{i1}) = \alpha_i + x'_i\beta \quad \log(\mu_{i2}) = \alpha_i, \quad (2)$$

for $j = 1, 2$ and $i = 1, \dots, k$. The sufficient statistics for the α_i are $y_{i1} + y_{i2} = y_{i+}$. Then it is easy to show that the conditional distribution of $y_{i1}|y_{i+}$ is precisely the model given by (1) where

$$\begin{aligned} p_i &= \mu_{i1}/\mu_{i+} \\ b_i &= y_{i1} \\ n_i &= y_{i+}. \end{aligned}$$

Therefore, conditioning out the nuisance parameters $\{\alpha_i\}$ and β for the Poisson log-linear model yields exactly the same (null) conditional distribution as conditioning out β in model (1). Furthermore, this exercise indicates exactly how to perform the calculations, which is useful since `exactLoglinTest` only accepts models in the form of Poisson log-linear models.

Currently `exactLoglinTest` is useful for tests of $\gamma = 0$. With modifications, the central ideas could be used to calculate a Monte Carlo estimate of the conditional likelihood for γ . (It is possible to use `mcexact` as is for this purpose. However, we have had mixed success in this endeavor and it is best avoided due to numerical instability.)

2 exactLoglinTest

The software `exactLoglinTest` is an implementation of the algorithms presented in [2] and [3]. At the heart of both algorithms is a sequentially generated rounded normal approximation to the conditional distribution. We refer the reader to those papers for a more complete description.

You can obtain a copy of `exactLoglinTest` as well as a no-web [6] version of this document at

<http://www.biostat.jhsph.edu/~bcaffo/downloads.htm>

You can install `exactLoglinTest` with R CMD `INSTALL`, on Unix and Linux, while the binaries are available for Windows. Assuming it is installed, one can load `mcexact` with

```
> library(exactLoglinTest)
> set.seed(1)
```

Here, the optional argument `lib.loc` is necessary if the package has been installed into one of the paths that R automatically checks. We also set the random number seed to a specific value which is a good practice for Monte Carlo procedures.

3 Examples

3.1 Residency Data

Assuming `exactLoglinTest` has been properly installed, the residency data can be obtained by the command

```
> data(residence.dat)
```

This data is a 4×4 table of persons' residence in 1985 by their residence in 1980. See Table 1 for the complete data. The data frame, `residence.dat`, contains the counts stacked by the rows. The extra term `sym.pair` is used to fit a quasi-symmetry model. For details on the quasi-symmetry model see [1]. To obtain a Monte Carlo goodness of fit test of quasi-symmetry versus a saturated model involves the following command

```

> resid.mcx <- mcexact(y ~ res.1985 + res.1980 + factor(sym.pair),
+                       data = residence.dat,
+                       nosim = 10 ^ 2,
+                       maxiter = 10 ^ 4)
> resid.mcx

```

```

              deviance    Pearson
observed.stat 2.98596233 2.98198696
pvalue         0.43615976 0.43615976
mcse           0.03240488 0.03240488

```

The default method is the importance sampling of [2]. Using this method, the number of desired simulations `nosim` may not be met in `maxiter` iterations and no warning is issued if this occurs. The returned value is a list storing the results of the Monte Carlo simulation and all of the relevant information necessary to restart the simulation. More information can be obtained with `summary`

```

> summary(resid.mcx)

```

```

$conde1

```

```

      15      14      10
294.8800 166.8939 238.3175

```

```

$condv1

```

```

 56.78443 -39.34468 36.79749
-39.34468 51.14382 -39.59345
 36.79749 -39.59345 59.74533

```

```

$dens

```

```

function (y)
sum(-lgamma(y + 1))
<environment: namespace:exactLoglinTest>

```

```

$dobs

```

```

[1] 2.985962 2.981987

```

```

$mu.hat

```

```

      15      14      10      16      13      12
 294.87999 166.89392 238.31746 10192.00000 63.22609 261.12001
      11      9      8      7      6      5
17819.00000 167.56253 311.10608 501.68254 13677.00000 91.21138
      4      3      2      1
 123.77391 370.43747 95.78862 11607.00000

```

```

$n

```

```

[1] 16

```

```

$n1

```

```

[1] 3

```

```

$nosim

```

```

[1] 100

```

```

$s

```

```

              [,1]
(Intercept) 55981
res.1985NE  11929
res.1985S   18986
res.1985W   10888

```

```

res.1980NE      12197
res.1980S      18486
res.1980W      10717
factor(sym.pair)2  187
factor(sym.pair)3  538
factor(sym.pair)4  187
factor(sym.pair)5 13677
factor(sym.pair)6   740
factor(sym.pair)8 17819

```

```
$stat
```

```

function (y = NULL, mu = NULL, rowlabels = FALSE)
{
  if (rowlabels)
    c("deviance", "Pearson")
  else {
    temp <- y != 0
    c(2 * sum(y[temp] * log(y[temp]/mu[temp])), sum((y -
      mu)^2/mu))
  }
}

```

```
<environment: namespace:exactLoglinTest>
```

```
$tdf
```

```
[1] 3
```

```
$x
```

	(Intercept)	res.1985NE	res.1985S	res.1985W	res.1980NE	res.1980S	res.1980W
15	1	0	1	0	0	0	1
14	1	0	0	0	0	0	1
10	1	0	0	0	0	1	0
16	1	0	0	1	0	0	1
13	1	1	0	0	0	0	1
12	1	0	0	1	0	1	0
11	1	0	1	0	0	1	0
9	1	1	0	0	0	1	0
8	1	0	0	1	0	0	0
7	1	0	1	0	0	0	0
6	1	0	0	0	0	0	0
5	1	1	0	0	0	0	0
4	1	0	0	1	1	0	0
3	1	0	1	0	1	0	0
2	1	0	0	0	1	0	0
1	1	1	0	0	1	0	0

	factor(sym.pair)2	factor(sym.pair)3	factor(sym.pair)4	factor(sym.pair)5
15	0	0	0	0
14	0	0	0	0
10	0	0	0	0
16	0	0	0	0
13	0	0	1	0
12	0	0	0	0
11	0	0	0	0
9	0	1	0	0
8	0	0	0	0
7	0	0	0	0
6	0	0	0	1
5	1	0	0	0
4	0	0	1	0

3	0	1	0	0
2	1	0	0	0
1	0	0	0	0
factor(sym.pair)6 factor(sym.pair)8				
15	0	0		
14	0	0		
10	1	0		
16	0	0		
13	0	0		
12	0	0		
11	0	1		
9	0	0		
8	0	0		
7	1	0		
6	0	0		
5	0	0		
4	0	0		
3	0	0		
2	0	0		
1	0	0		

\$x1

	(Intercept)	res.1985NE	res.1985S	res.1985W	res.1980NE	res.1980S	res.1980W
15	1	0	1	0	0	0	1
14	1	0	0	0	0	0	1
10	1	0	0	0	0	1	0
factor(sym.pair)2 factor(sym.pair)3 factor(sym.pair)4 factor(sym.pair)5							
15	0		0		0		0
14	0		0		0		0
10	0		0		0		0
factor(sym.pair)6 factor(sym.pair)8							
15	0		0				
14	0		0				
10	1		0				

\$x2invt

	(Intercept)	res.1985NE	res.1985S	res.1985W	res.1980NE	res.1980S	res.1980W
16	-1	0.5	0	1	0.5	0	1
13	1	-0.5	0	-1	-0.5	0	0
12	0	0.0	1	0	0.0	1	0
11	0	0.0	0	0	0.0	0	0
9	0	0.0	-1	0	0.0	0	0
8	2	-1.0	-1	-1	-1.0	-1	-1
7	0	0.0	0	0	0.0	0	0
6	0	0.0	0	0	0.0	0	0
5	-1	1.0	1	1	0.0	0	0
4	-1	0.5	0	1	0.5	0	0
3	0	0.0	1	0	0.0	0	0
2	1	-1.0	-1	-1	0.0	0	0
1	0	0.5	0	0	0.5	0	0
factor(sym.pair)2 factor(sym.pair)3 factor(sym.pair)4 factor(sym.pair)5							
16	0.5		0.5		-0.5		1
13	-0.5		-0.5		0.5		-1
12	0.0		-1.0		0.0		0
11	0.0		0.0		0.0		0
9	0.0		1.0		0.0		0
8	-1.0		0.0		0.0		-2
7	0.0		0.0		0.0		0

```

6          0.0          0.0          0.0          1
5          1.0          0.0          0.0          1
4          0.5          0.5          0.5          1
3          0.0          0.0          0.0          0
2          0.0          0.0          0.0          -1
1         -0.5         -0.5         -0.5          0

```

```

factor(sym.pair)6 factor(sym.pair)8
16          1          1
13         -1         -1
12         -1         -2
11          0          1
9           1          1
8          -1          0
7           1          0
6           0          0
5           0          0
4           1          1
3          -1         -1
2           0          0
1           0          0

```

\$y

```

15  14  10  16  13  12  11  9  8  7  6  5  4
286 176 225 10192 63 270 17819 172 302 515 13677 87 124
3 2 1
366 100 11607

```

\$ord

```
[1] 15 14 10 16 13 12 11 9 8 7 6 5 4 3 2 1
```

\$glm.fit

```
Call: glm(formula = formula, family = poisson, data = data, x = TRUE,
y = TRUE)
```

Coefficients:

```

(Intercept)          res.1985NE          res.1985S          res.1985W
      1.6281          3.8411          0.5692          4.1120
res.1980NE          res.1980S          res.1980W factor(sym.pair)2
      3.8901         -0.1752          3.4892         -0.9561
factor(sym.pair)3 factor(sym.pair)4 factor(sym.pair)5 factor(sym.pair)6
      -0.1728         -4.8118          7.8953          4.0206
factor(sym.pair)7 factor(sym.pair)8 factor(sym.pair)9 factor(sym.pair)10
           NA          7.7658           NA           NA

```

Degrees of Freedom: 15 Total (i.e. Null); 3 Residual

Null Deviance: 131000

Residual Deviance: 2.986 AIC: 159.2

\$maxiter

```
[1] 10000
```

\$startiter

```
[1] 101
```

\$sumdw

```
[1] 18.64563 18.64563
```

```

$sumdwsq
[1] 19.12212 19.12212

$sumw
[1] 42.74954

$sumwsq
[1] 42.36458

$impconst
[1] -466390.4

$phat
[1] 0.4361598 0.4361598

$mcse
[1] 0.03240488 0.03240488

$perpos
[1] 1

attr("class")
[1] "babSummary"

```

The t degrees of freedom refers to degrees of freedom used as a tuning parameter within the algorithm while the df refers to the model degrees of freedom. In this case, the Monte Carlo standard error, `mcse`, seems too large. As mentioned previously, `mcexact`, stores the relevant information for restarting the simulation

```

> resid.mcx <- update(resid.mcx, nosim = 10 ^ 4, maxiter = 10 ^ 6)
> resid.mcx

```

	deviance	Pearson
observed.stat	2.985962330	2.981986964
pvalue	0.400636040	0.400930887
mcse	0.003196472	0.003196835

It is important to note that `update` only resumes the simulation with changes to simulation-specific parameters. It will not allow users to change the model formulation; one must rerun `mcexact` independently to do that.

This example illustrates the point that the underlying algorithms are very efficient when the cell counts are large. Of course, when this is the case, the large sample approximations are nearly identical to the conditional results

```

> pchisq(c(2.986, 2.982), 3, lower.tail = FALSE)

[1] 0.3937887 0.3944088

```

3.2 Pathologists' Tumor Ratings

The following example is interesting in that the large sample results differ drastically from the conditional results. Moreover, the conditional results are less conservative. The data, given in Table 2 can be obtained via

```

> data(pathologist.dat)

```

A uniform association model accounts for the ordinal nature of the ratings by associating ordinal scores with the pathologist's ratings [see 1]. Specifically, we can test a uniform association model against the saturated model with

```

> path.mcx <- mcexact(y ~ factor(A) + factor(B) + I(A * B),
+                   data = pathologist.dat,
+                   nosim = 10 ^ 4,
+                   maxiter = 10 ^ 4)
> summary(path.mcx)

```

\$conde1

	20	19	18	17	15	14
6.344616e-01	3.692094e+00	1.749242e+01	1.770945e-01	2.998565e-02	1.123799e+00	
	13	12	10	9	8	25
3.429048e+01	2.235819e+00	3.025095e-04	7.301670e-02	1.434878e+01	2.335250e+00	
	24	23	22			
2.110050e+00	1.552251e+00	2.440110e-03				

\$condv1

3.992947e-01	-1.512630e-01	-0.2302951722	-1.683236e-02	-1.354645e-02
-1.512630e-01	1.285627e+00	-1.1337928058	-9.767044e-04	-2.392629e-03
-2.302952e-01	-1.133793e+00	1.5130688567	-1.460797e-01	1.802070e-02
-1.683236e-02	-9.767044e-04	-0.1460797229	1.643946e-01	-1.958202e-03
-1.354645e-02	-2.392629e-03	0.0180207042	-1.958202e-03	2.886289e-02
-8.111453e-02	-5.988614e-01	0.6966776416	-1.548698e-02	-1.038945e-02
1.894272e-01	4.925053e-01	-0.8031364378	1.162690e-01	-2.453056e-03
-5.915681e-02	7.589214e-02	0.0632142608	-7.761053e-02	-1.042780e-02
-1.685691e-04	-3.183465e-06	0.0002077854	-3.388633e-05	-1.587280e-05
-9.327963e-03	-3.675231e-02	0.0488399809	-2.572783e-03	-1.225006e-03
-2.138232e-03	6.014399e-02	-0.1636048047	1.032278e-01	-1.557045e-03
-3.855792e-01	1.536587e-01	0.2120661394	1.882458e-02	-1.530052e-02
2.419696e-01	-6.495954e-01	0.3874878075	1.913509e-02	1.404431e-02
1.437071e-01	4.949123e-01	-0.5989177210	-3.768255e-02	1.302339e-03
-9.565519e-05	1.019615e-03	-0.0006350826	-2.754771e-04	-4.573679e-05
-0.0811145281	0.1894272278	-0.0591568137	-1.685691e-04	-9.327963e-03
-0.5988613532	0.4925052899	0.0758921360	-3.183465e-06	-3.675231e-02
0.6966776416	-0.8031364378	0.0632142608	2.077854e-04	4.883998e-02
-0.0154869817	0.1162689632	-0.0776105282	-3.388633e-05	-2.572783e-03
-0.0103894478	-0.0024530562	-0.0104277955	-1.587280e-05	-1.225006e-03
0.7869316765	-0.5710434774	-0.1405318761	-1.493944e-04	-2.672783e-02
-0.5710434774	1.7623815394	-1.1342630814	3.904828e-04	4.405264e-02
-0.1405318761	-1.1342630814	1.4174614975	-1.347161e-04	-8.302405e-03
-0.0001493944	0.0003904828	-0.0001347161	3.022609e-04	-2.146740e-05
-0.0267278342	0.0440526416	-0.0083024047	-2.146740e-05	6.998117e-02
-0.0268356441	-1.4105516405	1.2509438439	-2.596956e-04	-6.002243e-02
0.0916538934	-0.1873660854	0.0697198468	-1.178181e-04	1.057451e-02
-0.1607465057	0.0332474968	0.0732946813	1.746923e-04	-6.426580e-03
0.0694956953	0.1515129370	-0.1414406076	-5.596201e-05	-4.068555e-03
-0.0003991607	0.0025894889	-0.0015662853	-9.049401e-07	-7.872439e-05
-0.0021382316	-0.3855791564	0.2419696249	1.437071e-01	-9.565519e-05
0.0601439882	0.1536587142	-0.6495953877	4.949123e-01	1.019615e-03
-0.1636048047	0.2120661394	0.3874878075	-5.989177e-01	-6.350826e-04
0.1032278276	0.0188245778	0.0191350909	-3.768255e-02	-2.754771e-04
-0.0015570454	-0.0153005192	0.0140443088	1.302339e-03	-4.573679e-05
-0.0268356441	0.0916538934	-0.1607465057	6.949570e-02	-3.991607e-04
-1.4105516405	-0.1873660854	0.0332474968	1.515129e-01	2.589489e-03
1.2509438439	0.0697198468	0.0732946813	-1.414406e-01	-1.566285e-03
-0.0002596956	-0.0001178181	0.0001746923	-5.596201e-05	-9.049401e-07
-0.0600224324	0.0105745120	-0.0064265799	-4.068555e-03	-7.872439e-05
2.4262895610	0.0039554188	0.0273610511	-3.269460e-02	1.373295e-03


```

0.0039554188 0.4009976184 -0.2561891403 -1.449531e-01 1.423006e-04
0.0273610511 -0.2561891403 0.8167173280 -5.599893e-01 -5.387153e-04
-0.0326945978 -0.1449530621 -0.5599893053 7.069878e-01 -2.034924e-03
0.0013732947 0.0001423006 -0.0005387153 -2.034924e-03 2.431391e-03

```

```

$dens
function (y)
sum(-lgamma(y + 1))
<environment: namespace:exactLoglinTest>

```

```

$dobs
[1] 16.21453 14.72928

```

```

$mu.hat
      20      19      18      17      15      14
6.344616e-01 3.692094e+00 1.749242e+01 1.770945e-01 2.998565e-02 1.123799e+00
      13      12      10      9      8      25
3.429048e+01 2.235819e+00 3.025095e-04 7.301670e-02 1.434878e+01 2.335250e+00
      24      23      22      21      16      11
2.110050e+00 1.552251e+00 2.440110e-03 8.417609e-06 3.934524e-03 3.199129e-01
      7      6      5      4      3      2
6.025400e+00 5.552502e+00 6.689408e-07 1.039869e-03 1.316071e+00 3.559247e+00
      1
2.112364e+01

```

```

$n
[1] 25

```

```

$n1
[1] 15

```

```

$nosim
[1] 10000

```

```

$s
      [,1]
(Intercept) 118
factor(A)2   12
factor(A)3   69
factor(A)4    7
factor(A)5    3
factor(B)2   26
factor(B)3   38
factor(B)4   22
factor(B)5    6
I(A * B)    898

```

```

$stat
function (y = NULL, mu = NULL, rowlabels = FALSE)
{
  if (rowlabels)
    c("deviance", "Pearson")
  else {
    temp <- y != 0
    c(2 * sum(y[temp] * log(y[temp]/mu[temp])), sum((y -
      mu)^2/mu))
  }
}

```

```
<environment: namespace:exactLoglinTest>
```

```
$tdf  
[1] 3
```

```
$x
```

	(Intercept)	factor(A)2	factor(A)3	factor(A)4	factor(A)5	factor(B)2
20	1	0	0	0	1	0
19	1	0	0	1	0	0
18	1	0	1	0	0	0
17	1	1	0	0	0	0
15	1	0	0	0	1	0
14	1	0	0	1	0	0
13	1	0	1	0	0	0
12	1	1	0	0	0	0
10	1	0	0	0	1	1
9	1	0	0	1	0	1
8	1	0	1	0	0	1
25	1	0	0	0	1	0
24	1	0	0	1	0	0
23	1	0	1	0	0	0
22	1	1	0	0	0	0
21	1	0	0	0	0	0
16	1	0	0	0	0	0
11	1	0	0	0	0	0
7	1	1	0	0	0	1
6	1	0	0	0	0	1
5	1	0	0	0	1	0
4	1	0	0	1	0	0
3	1	0	1	0	0	0
2	1	1	0	0	0	0
1	1	0	0	0	0	0

	factor(B)3	factor(B)4	factor(B)5	I(A * B)
20	0	1	0	20
19	0	1	0	16
18	0	1	0	12
17	0	1	0	8
15	1	0	0	15
14	1	0	0	12
13	1	0	0	9
12	1	0	0	6
10	0	0	0	10
9	0	0	0	8
8	0	0	0	6
25	0	0	1	25
24	0	0	1	20
23	0	0	1	15
22	0	0	1	10
21	0	0	1	5
16	0	1	0	4
11	1	0	0	3
7	0	0	0	4
6	0	0	0	2
5	0	0	0	5
4	0	0	0	4
3	0	0	0	3
2	0	0	0	2
1	0	0	0	1

\$x1

	(Intercept)	factor(A)2	factor(A)3	factor(A)4	factor(A)5	factor(B)2
20	1	0	0	0	1	0
19	1	0	0	1	0	0
18	1	0	1	0	0	0
17	1	1	0	0	0	0
15	1	0	0	0	1	0
14	1	0	0	1	0	0
13	1	0	1	0	0	0
12	1	1	0	0	0	0
10	1	0	0	0	1	1
9	1	0	0	1	0	1
8	1	0	1	0	0	1
25	1	0	0	0	1	0
24	1	0	0	1	0	0
23	1	0	1	0	0	0
22	1	1	0	0	0	0

	factor(B)3	factor(B)4	factor(B)5	I(A * B)
20	0	1	0	20
19	0	1	0	16
18	0	1	0	12
17	0	1	0	8
15	1	0	0	15
14	1	0	0	12
13	1	0	0	9
12	1	0	0	6
10	0	0	0	10
9	0	0	0	8
8	0	0	0	6
25	0	0	1	25
24	0	0	1	20
23	0	0	1	15
22	0	0	1	10

\$x2invt

	(Intercept)	factor(A)2	factor(A)3	factor(A)4	factor(A)5	factor(B)2
21	0	0	0	0	0	0
16	0	0	0	0	0	0
11	0	0	0	0	0	0
7	-1	-1	-2	-3	-4	-1
6	1	1	2	3	4	2
5	0	0	0	0	1	0
4	0	0	0	1	0	0
3	0	0	1	0	0	0
2	1	2	2	3	4	1
1	0	-2	-3	-4	-5	-2

	factor(B)3	factor(B)4	factor(B)5	I(A * B)
21	0	0	1	0
16	0	1	0	0
11	1	0	0	0
7	-2	-3	-4	1
6	2	3	4	-1
5	0	0	0	0
4	0	0	0	0
3	0	0	0	0
2	2	3	4	-1
1	-3	-4	-5	1

```

$y
20 19 18 17 15 14 13 12 10 9 8 25 24 23 22 21 16 11 7 6 5 4 3 2 1
0 7 14 1 0 0 36 2 0 0 14 3 0 3 0 0 0 0 7 5 0 0 2 2 22

$ord
[1] 20 19 18 17 15 14 13 12 10 9 8 25 24 23 22 21 16 11 7 6 5 4 3 2 1

$glm.fit

Call: glm(formula = formula, family = poisson, data = data, x = TRUE,
y = TRUE)

Coefficients:
(Intercept) factor(A)2 factor(A)3 factor(A)4 factor(A)5 factor(B)2
1.188 -3.643 -6.501 -15.507 -24.718 -3.199
factor(B)3 factor(B)4 factor(B)5 I(A * B)
-7.915 -14.176 -22.186 1.863

Degrees of Freedom: 24 Total (i.e. Null); 15 Residual
Null Deviance: 267.7
Residual Deviance: 16.21 AIC: 82.48

$maxiter
[1] 10000

$startiter
[1] 1

$sumdw
[1] 0

$sumdwsq
[1] 0

$sumw
[1] 0

$sumwsq
[1] 0

$phat
[1] NaN

$mcse
[1] NaN

$perpos
[1] 0

attr(,"class")
[1] "babSummary"

```

The previous code chunk takes about 1 minute on my laptop. It is worth comparing these results to the asymptotic Chi-squared results

```

> pchisq(c(16.214, 14.729), 15, lower.tail = FALSE)
[1] 0.3679734 0.4711083

```

3.3 Alligator Food Choice Data Using MCMC

In this example we illustrate the algorithm from [3] using the data and Poisson log-linear model from Table 3. The alligator data is a good choice for MCMC as the percent of valid tables generated using `method = "bab"` is very small, less than 1% of the tables simulated. It is often the case that the MCMC algorithm will be preferable when the table is large and/or sparse. Of course, using MCMC introduces further complications in reliably running and using the output of the algorithm.

The algorithm from [3] uses local moves to reduce the number of tables with negative entries that the chain produces. You can specify this method by using `method = "cab"`. The parameter `p` represents the average proportion of table entries left fixed. So a chain with `p=.9` will leave most of the table entries fixed from one iteration to the next. A high value of `p` will result in a high proportion of valid (non-negative) simulated tables. Too large of a value of `p` causes the chain to mix slowly because the tables will be very similar from one iteration to the next. However, it is sometimes the case that a small value of `p` will produce too many tables with negative entries. Hence the Metropolis/Hastings/Green algorithm will stay at the current table for long periods and again result in a slowly mixing chain. It is also worth mentioning that for large values of `p` the algorithm is theoretically irreducible, but may not be practically irreducible. Therefore, it is advisable to both tinker with the chain some and make final runs using multiple values of `p`.

The program allows for the option to save the chain goodness of fit statistics, so that some initial tinkering can be performed. This is specified with the `savechain = TRUE` option. If using importance sampling, `method = "bab"`, then `savechain` saves both the statistic values and the importance weights on the log scale.

```
> data(alligator.dat)
> alligator.mcx <- mcexact(y ~ (lake + gender + size) * food + lake * gender * size,
+                          data = alligator.dat,
+                          nosim = 10 ^ 3,
+                          method = "cab",
+                          savechain = TRUE,
+                          batchsize = 100,
+                          p = .4)
> summary(alligator.mcx)
```

\$conde1

	75	74	73	72	70	69	68
1.31600087	0.48346172	0.18073692	6.51660315	1.13800295	0.81453108	0.25072319	
	67	60	59	58	57	55	54
1.60473559	0.18105409	0.13394981	0.26096632	0.21080481	1.97444067	0.52630855	
	53	52	50	49	48	47	40
1.21928164	6.54106633	5.63440188	2.92618991	5.58172191	5.31553870	0.13185304	
	39	38	37	35	34	33	32
0.07554443	0.51708045	0.55718074	0.79011836	0.16310491	1.32752883	9.50014868	
	30	29	28	27	20	19	18
1.78879234	0.71943767	4.82138891	6.12481782	1.78671996	1.50458067	0.82331031	
	17	80	79	78	77		
0.24350239	1.03386967	1.05416634	0.33141537	1.79927933			

\$condv1

0.8158428899	-4.024685e-02	-1.553110e-02	-0.349190606	-0.1432926821			
-0.0402468520	3.425437e-01	-6.423501e-03	-0.132000575	0.0112669026			
-0.0155310983	-6.423501e-03	1.418543e-01	-0.056732328	0.0054324960			
-0.3491906063	-1.320006e-01	-5.673233e-02	1.944240192	0.0541580685			
-0.1432926821	1.126690e-02	5.432496e-03	0.054158069	0.7401576216			
0.0126479801	-6.698040e-02	2.194671e-03	0.021894398	-0.0553905322			
0.0051999933	1.668882e-03	-4.001101e-02	0.018815577	-0.0196291578			
0.0427174386	1.701258e-02	1.118021e-02	-0.206501050	-0.1424549232			
-0.0107478602	9.515460e-04	3.247559e-04	0.007024218	-0.0004989307			
0.0009304963	-5.024699e-03	2.000605e-04	0.004639496	-0.0013730257			

0.0020305479	1.354304e-03	-1.518614e-03	-0.002545615	-0.0007124931
0.0045797255	1.497876e-03	5.267360e-04	-0.023797868	0.0028035524
-0.1980993866	6.075710e-03	5.407843e-03	0.184127587	0.1496365772
0.0078073066	-6.873110e-02	1.977967e-03	0.056534616	-0.0136143474
0.0102063142	2.962669e-03	-3.255049e-02	0.042264127	-0.0142522175
0.1366844470	4.568478e-02	1.659121e-02	-0.517973431	-0.0627665744
0.1993899950	-1.367119e-02	-9.238751e-03	-0.110748159	-0.2337196537
-0.0140866155	9.559156e-02	-3.555370e-03	-0.054177923	0.0183523013
-0.0188685469	-7.591748e-03	4.410161e-02	-0.012509049	0.0190353775
-0.0920784386	-4.329516e-02	-1.459001e-02	0.361106082	0.0891353606
-0.0080752925	1.324869e-04	2.071072e-04	0.004468277	-0.0004131863
-0.0003415250	-3.020569e-03	9.053576e-05	0.002609869	-0.0006105333
-0.0016771963	2.878589e-05	-2.867681e-03	-0.003494169	-0.0009174062
0.0074260713	2.258904e-03	1.114944e-03	-0.050775447	0.0030639985
-0.0849167457	-2.050967e-03	1.872812e-03	0.068924106	0.0719471826
-0.0003087532	-2.193521e-02	5.410853e-04	0.017323964	-0.0013128616
-0.0105051563	-5.477681e-03	-3.527090e-02	0.048514814	0.0065273111
0.0687785132	2.385286e-02	1.798516e-02	-0.556154021	-0.0165875622
0.0895235521	1.612037e-03	-2.541660e-03	-0.056763707	-0.0857398927
0.0001866741	2.717585e-02	-7.686077e-04	-0.018541918	0.0017031657
0.0102985658	5.228012e-03	4.154175e-02	-0.030921208	-0.0082281417
-0.0562173667	-2.215968e-02	-1.715349e-02	0.505456857	0.0177359687
-0.0052008245	-7.118337e-03	-2.684526e-04	0.004642330	-0.0863596513
-0.0037068574	3.700360e-02	-1.540702e-03	-0.015858387	0.0046324516
0.0008862818	-2.389580e-03	6.526212e-03	-0.009244601	0.0021926126
0.0022527803	-1.239194e-03	2.709523e-04	-0.010948376	0.0042210349
-0.2410652748	1.935201e-02	6.659537e-03	0.082691382	-0.2126596733
0.0155880999	-1.594698e-01	3.834239e-03	0.056894076	0.0217753875
0.0064294250	4.752970e-03	-5.802036e-02	0.013744369	0.0068771464
0.0956599413	4.855803e-02	1.879302e-02	-0.603778526	0.0232833502
0.0126479801	0.0051999933	0.0427174386	-0.0107478602	9.304963e-04
-0.0669804029	0.0016688823	0.0170125805	0.0009515460	-5.024699e-03
0.0021946710	-0.0400110088	0.0111802099	0.0003247559	2.000605e-04
0.0218943983	0.0188155772	-0.2065010499	0.0070242177	4.639496e-03
-0.0553905322	-0.0196291578	-0.1424549232	-0.0004989307	-1.373026e-03
0.4699468498	-0.0123104240	-0.0821830095	-0.0022970012	1.151175e-02
-0.0123104240	0.1777975938	-0.0324663406	-0.0010022218	-1.121173e-03
-0.0821830095	-0.0324663406	1.0664840652	0.0033920589	-2.549591e-04
-0.0022970012	-0.0010022218	0.0033920589	0.1407906696	-2.286272e-02
0.0115117504	-0.0011211725	-0.0002549591	-0.0228627205	1.069917e-01
-0.0034299062	0.0045169851	0.0030080740	-0.0420030278	-3.002572e-02
-0.0020880710	-0.0008521845	-0.0088988247	-0.0374788962	-2.663943e-02
-0.0133854403	-0.0085222713	-0.0618389683	-0.0462481557	5.159438e-03
0.0922495421	-0.0037306178	-0.0296581971	0.0056789335	-2.767602e-02
-0.0064150666	0.0406810936	-0.0145578408	0.0147496924	9.484085e-03
-0.0410168313	-0.0138090712	0.2110348280	0.0191931125	1.080015e-02
0.0189441710	0.0105416530	0.0975417670	-0.0913671295	1.576411e-02
-0.1193893942	0.0050729944	0.0404832621	0.0160377018	-7.596599e-02
0.0107283400	-0.0487382052	0.0166439096	0.0322719142	2.399055e-02
0.0403061795	0.0114673746	-0.3465284760	0.0183331781	1.530134e-02
-0.0003138193	-0.0006671666	0.0027339907	-0.0032659214	-1.864083e-05
0.0067659440	-0.0005726100	0.0000333626	0.0001957909	-2.969134e-03
-0.0009585807	0.0081423905	0.0068915377	0.0059071292	4.404260e-03
-0.0011963837	-0.0020195148	-0.0188973131	-0.0003265022	8.651739e-05
0.0010770017	-0.0028448799	-0.0308240999	-0.0048706854	3.978516e-04
0.0288261683	-0.0009880553	-0.0103895660	0.0006047980	-3.078922e-03
0.0051290539	0.0425381838	-0.0263261141	0.0054666140	4.126056e-03

-0.0064310939 -0.0138033770 0.2932539021 -0.0020637710 -6.395668e-04
-0.0010315134 0.0035525044 0.0344151709 0.0029796051 -3.912278e-04
-0.0369965501 0.0015564646 0.0115881677 -0.0007040545 4.921347e-03
-0.0049868857 -0.0513676031 0.0227106812 -0.0075922700 -6.167792e-03
0.0067072418 0.0135653298 -0.3489096838 0.0056361985 1.550741e-03
0.0007924853 -0.0005548973 -0.0040734208 -0.0302563131 7.942514e-03
-0.0072037068 -0.0015637203 -0.0052136601 0.0075861027 -3.075352e-02
-0.0007833930 0.0003018796 -0.0123086040 0.0104799047 8.203715e-03
0.0008049234 -0.0001603018 -0.0268160003 0.0014269821 1.287728e-03
0.0244478758 0.0079935766 0.0250158238 -0.0233704312 4.201409e-03
-0.2191987175 0.0075580068 0.0330149286 0.0052909104 -2.827038e-02
0.0080217961 -0.0770320848 0.0089504876 0.0043979191 3.485831e-03
0.0353895251 0.0107155495 -0.2959519775 0.0087738144 8.881541e-03

0.0020305479 0.0045797255 -1.980994e-01 0.0078073066 0.0102063142
0.0013543036 0.0014978761 6.075710e-03 -0.0687311011 0.0029626691
-0.0015186139 0.0005267360 5.407843e-03 0.0019779671 -0.0325504915
-0.0025456149 -0.0237978676 1.841276e-01 0.0565346157 0.0422641267
-0.0007124931 0.0028035524 1.496366e-01 -0.0136143474 -0.0142522175
-0.0034299062 -0.0020880710 -1.338544e-02 0.0922495421 -0.0064150666
0.0045169851 -0.0008521845 -8.522271e-03 -0.0037306178 0.0406810936
0.0030080740 -0.0088988247 -6.183897e-02 -0.0296581971 -0.0145578408
-0.0420030278 -0.0374788962 -4.624816e-02 0.0056789335 0.0147496924
-0.0300257241 -0.0266394265 5.159438e-03 -0.0276760239 0.0094840853
0.1718084526 -0.0494526993 1.537225e-02 0.0077831025 -0.0607035817
-0.0494526993 0.1585909826 1.904074e-02 0.0088418845 0.0215914319
0.0153722508 0.0190407350 9.145374e-01 -0.0668014199 -0.1176860809
0.0077831025 0.0088418845 -6.680142e-02 0.3215796804 -0.0370742254
-0.0607035817 0.0215914319 -1.176861e-01 -0.0370742254 0.6085968528
0.0278206701 -0.0663303568 -4.807257e-01 -0.1381671907 -0.3107271639
0.0312802546 0.0191538978 -4.635803e-01 0.0495094373 0.0711436767
0.0225639360 0.0172948393 4.854106e-02 -0.2137723814 0.0235998902
-0.1307969846 0.0344243907 6.743091e-02 0.0239238152 -0.3683467327
0.0343035956 -0.0917555929 1.713166e-01 0.0650401894 0.1565394565
0.0026361368 0.0005520898 -1.233563e-02 0.0005286044 0.0050599043
0.0018306898 0.0005905866 8.828207e-05 -0.0068328922 0.0029809887
-0.0269601665 0.0085506529 8.740781e-03 0.0027425457 -0.0521044107
0.0100231951 -0.0099735877 7.719214e-03 0.0028308240 0.0176508644
0.0029767060 0.0003022203 -1.638771e-01 0.0012566405 0.0285369530
0.0011702958 0.0004960990 5.296996e-04 -0.0342591332 0.0060393209
-0.0216164891 0.0043688967 3.849739e-02 0.0104258340 -0.3055965349
0.0078809809 -0.0076458349 1.668007e-01 0.0455489802 0.1953557053
-0.0041195445 0.0022932975 1.764678e-01 -0.0027174578 -0.0373721063
-0.0026895340 -0.0005066030 -1.233410e-03 0.0432829004 -0.0098612167
0.0300545227 -0.0053338500 -5.242853e-02 -0.0153484186 0.3636482428
-0.0049405014 -0.0047913569 -1.543108e-01 -0.0464030121 -0.1943050371
0.0110257996 0.0031221958 2.323909e-02 -0.0095204502 -0.0065092455
0.0104701647 0.0049723134 -7.438347e-03 0.0245082784 -0.0046016531
-0.0395963274 0.0089755435 -4.592797e-03 -0.0046054720 0.0056462534
0.0015435686 -0.0054937043 -1.777478e-03 -0.0020498769 0.0005614384
0.0040343291 0.0075599150 -4.487586e-02 0.0031110794 0.0013684638
0.0063176806 0.0083299532 3.964997e-03 -0.0294235374 -0.0001360425
-0.0192634126 0.0053647356 3.678396e-03 0.0010115479 -0.0196713847
0.0052224958 -0.0372803569 3.207155e-02 0.0065124972 0.0160335874

0.136684447 0.199389995 -0.014086615 -0.018868547 -0.092078439 -8.075292e-03
0.045684776 -0.013671191 0.095591557 -0.007591748 -0.043295161 1.324869e-04
0.016591212 -0.009238751 -0.003555370 0.044101605 -0.014590006 2.071072e-04

-0.517973431 -0.110748159 -0.054177923 -0.012509049 0.361106082 4.468277e-03
 -0.062766574 -0.233719654 0.018352301 0.019035378 0.089135361 -4.131863e-04
 -0.041016831 0.018944171 -0.119389394 0.010728340 0.040306179 -3.138193e-04
 -0.013809071 0.010541653 0.005072994 -0.048738205 0.011467375 -6.671666e-04
 0.211034828 0.097541767 0.040483262 0.016643910 -0.346528476 2.733991e-03
 0.019193113 -0.091367130 0.016037702 0.032271914 0.018333178 -3.265921e-03
 0.010800152 0.015764113 -0.075965988 0.023990547 0.015301337 -1.864083e-05
 0.027820670 0.031280255 0.022563936 -0.130796985 0.034303596 2.636137e-03
 -0.066330357 0.019153898 0.017294839 0.034424391 -0.091755593 5.520898e-04
 -0.480725741 -0.463580280 0.048541056 0.067430908 0.171316639 -1.233563e-02
 -0.138167191 0.049509437 -0.213772381 0.023923815 0.065040189 5.286044e-04
 -0.310727164 0.071143677 0.023599890 -0.368346733 0.156539457 5.059904e-03
 1.503918926 0.164600551 0.071204797 0.167381313 -0.677100460 4.695245e-03
 0.164600551 1.252463499 -0.118296805 -0.192684682 -0.441662591 -5.307306e-03
 0.071204797 -0.118296805 0.518281932 -0.073402417 -0.148750150 -3.581620e-04
 0.167381313 -0.192684682 -0.073402417 0.893541760 -0.327086254 -6.944460e-04
 -0.677100460 -0.441662591 -0.148750150 -0.327086254 1.656756915 6.742172e-03
 0.004695245 -0.005307306 -0.000358162 -0.000694446 0.006742172 1.153530e-01
 0.002819630 -0.001191993 0.004659606 -0.001781557 0.000383091 -4.778090e-03
 0.026668139 -0.004665924 -0.005117530 -0.000641135 0.016926474 -2.800300e-02
 -0.037818899 0.013909448 0.002186016 0.009837101 -0.043887524 -3.571017e-02
 0.113147871 0.200781837 -0.003401055 -0.041407888 -0.114822249 -3.614297e-02
 0.024669704 -0.002426615 0.046490898 -0.009831266 -0.027328022 8.970305e-04
 0.195411776 -0.061092053 -0.019378781 0.391373453 -0.202173393 9.953006e-03
 -0.629165812 -0.154036446 -0.045847810 -0.219482742 0.674651768 1.532328e-02
 -0.107238921 -0.240634075 0.004451623 0.049488468 0.133139452 -7.117190e-02
 -0.027149146 0.003530685 -0.057050324 0.012666865 0.030896774 3.613956e-03
 -0.211227649 0.074212969 0.025406638 -0.456000489 0.219987481 1.867529e-02
 0.616341264 0.182605788 0.053147674 0.233946502 -0.789375048 1.723452e-02
 0.008999189 -0.260972246 0.033519295 0.043431156 0.063640040 -2.159670e-02
 -0.006044357 0.039851777 -0.102017679 0.013767105 0.011765222 2.062231e-03
 0.009181862 0.041829423 0.010906384 -0.121554621 0.019396283 6.943866e-03
 0.005061192 0.022461373 0.007449918 0.006761405 -0.060423423 1.216517e-03
 0.031157969 -0.120722284 0.002607279 0.006424957 0.067273836 -1.716722e-02
 0.015218451 -0.003257817 -0.014753543 -0.005901417 0.022821510 4.771677e-04
 0.009955762 0.003966056 -0.001104606 -0.026059722 0.014212452 2.790378e-03
 -0.085044651 0.090452799 0.021723403 0.022042148 -0.280304823 7.033318e-03

 -3.415250e-04 -1.677196e-03 7.426071e-03 -0.0849167457 -0.0003087532
 -3.020569e-03 2.878589e-05 2.258904e-03 -0.0020509665 -0.0219352061
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 6.765944e-03 -9.585807e-04 -1.196384e-03 0.0010770017 0.0288261683
 -5.726100e-04 8.142390e-03 -2.019515e-03 -0.0028448799 -0.0009880553
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 -1.781557e-03 -6.411350e-04 9.837101e-03 -0.0414078879 -0.0098312657
 3.830910e-04 1.692647e-02 -4.388752e-02 -0.1148222493 -0.0273280220

-4.778090e-03	-2.800300e-02	-3.571017e-02	-0.0361429717	0.0008970305
6.557929e-02	-1.547777e-02	-1.943793e-02	0.0005091210	-0.0138327064
-1.547777e-02	3.094219e-01	-1.160108e-01	0.0086907879	0.0031034165
-1.943793e-02	-1.160108e-01	3.637149e-01	0.0187296685	0.0059130901
5.091210e-04	8.690788e-03	1.872967e-02	0.4714766856	-0.0109139362
-1.383271e-02	3.103417e-03	5.913090e-03	-0.0109139362	0.1235097858
4.534662e-03	-1.187391e-01	5.381296e-02	-0.0587627701	-0.0147005706
6.292025e-03	6.539765e-02	-1.602430e-01	-0.2241175628	-0.0523788765
3.786937e-03	1.842151e-02	1.547241e-02	-0.3572279036	0.0102151810
-4.928482e-02	1.195804e-02	1.295517e-02	0.0104191045	-0.1018399168
1.147858e-02	-2.038041e-01	6.850122e-02	0.0475284349	0.0117377042
1.244720e-02	6.458735e-02	-2.018523e-01	0.1375360944	0.0355025428
2.937507e-03	1.182648e-02	-5.204105e-03	0.0299827004	-0.0025510328
-1.714947e-02	8.106909e-03	-1.073269e-03	-0.0028256827	0.0123298802
4.247656e-03	-6.979366e-02	2.168306e-02	-0.0045674867	-0.0019578378
8.056672e-04	3.830464e-03	-1.099984e-02	-0.0033860727	-0.0012352890
9.786888e-04	-9.057320e-04	6.515808e-03	-0.0042817885	0.0009671716
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5.290730e-03	1.466011e-02	-7.727823e-02	-0.0017998888	-0.0011907025
-1.050516e-02	0.0687785132	0.0895235521	0.0001866741	0.0102985658
-5.477681e-03	0.0238528552	0.0016120372	0.0271758486	0.0052280118
-3.527090e-02	0.0179851580	-0.0025416599	-0.0007686077	0.0415417484
4.851481e-02	-0.5561540208	-0.0567637067	-0.0185419176	-0.0309212077
6.527311e-03	-0.0165875622	-0.0857398927	0.0017031657	-0.0082281417
5.129054e-03	-0.0064310939	-0.0010315134	-0.0369965501	-0.0049868857
4.253818e-02	-0.0138033770	0.0035525044	0.0015564646	-0.0513676031
-2.632611e-02	0.2932539021	0.0344151709	0.0115881677	0.0227106812
5.466614e-03	-0.0020637710	0.0029796051	-0.0007040545	-0.0075922700
4.126056e-03	-0.0006395668	-0.0003912278	0.0049213471	-0.0061677919
-2.161649e-02	0.0078809809	-0.0041195445	-0.0026895340	0.0300545227
4.368897e-03	-0.0076458349	0.0022932975	-0.0005066030	-0.0053338500
3.849739e-02	0.1668007443	0.1764677727	-0.0012334100	-0.0524285293
1.042583e-02	0.0455489802	-0.0027174578	0.0432829004	-0.0153484186
-3.055965e-01	0.1953557053	-0.0373721063	-0.0098612167	0.3636482428
1.954118e-01	-0.6291658123	-0.1072389208	-0.0271491461	-0.2112276487
-6.109205e-02	-0.1540364458	-0.2406340750	0.0035306845	0.0742129688
-1.937878e-02	-0.0458478104	0.0044516231	-0.0570503236	0.0254066378
3.913735e-01	-0.2194827417	0.0494884681	0.0126668650	-0.4560004887
-2.021734e-01	0.6746517683	0.1331394519	0.0308967739	0.2199874812
9.953006e-03	0.0153232783	-0.0711719005	0.0036139558	0.0186752932
4.534662e-03	0.0062920249	0.0037869371	-0.0492848219	0.0114785772
-1.187391e-01	0.0653976471	0.0184215136	0.0119580358	-0.2038041110
5.381296e-02	-0.1602430177	0.0154724070	0.0129551724	0.0685012160
-5.876277e-02	-0.2241175628	-0.3572279036	0.0104191045	0.0475284349
-1.470057e-02	-0.0523788765	0.0102151810	-0.1018399168	0.0117377042
6.151768e-01	-0.3176066871	0.0471329342	0.0104320376	-0.4087806088
-3.176067e-01	1.4890769536	0.1447732782	0.0381692362	0.1813445124
4.713293e-02	0.1447732782	0.5789378210	-0.0164284063	-0.0825796375
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1.820352e-01	-0.8804246893	-0.2172358612	-0.0590512078	-0.3263102299
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-2.344774e-03	0.0001208034	0.0046388545	-0.0075583664	-0.0009470604
3.073025e-02	-0.0046902190	0.0043755897	-0.0007547275	-0.0230596792
-3.685949e-03	0.0224426879	0.0063491494	0.0013060650	0.0044479716
3.107155e-03	-0.0092669100	-0.0130457711	-0.0016307621	-0.0038912371

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-0.056217367 -0.0052008245 -0.0037068574 0.0008862818 0.0022527803
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0.505456857 0.0046423303 -0.0158583875 -0.0092446014 -0.0109483758
0.017735969 -0.0863596513 0.0046324516 0.0021926126 0.0042210349
0.006707242 0.0007924853 -0.0072037068 -0.0007833930 0.0008049234
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0.005636198 -0.0302563131 0.0075861027 0.0104799047 0.0014269821
0.001550741 0.0079425142 -0.0307535162 0.0082037154 0.0012877282
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0.182605788 -0.2609722460 0.0398517765 0.0418294234 0.0224613731
0.053147674 0.0335192947 -0.1020176794 0.0109063844 0.0074499184
0.233946502 0.0434311561 0.0137671048 -0.1215546210 0.0067614051
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0.017234520 -0.0215967030 0.0020622308 0.0069438657 0.0012165166
0.012447199 0.0029375071 -0.0171494739 0.0042476556 0.0008056672
0.064587352 0.0118264767 0.0081069094 -0.0697936618 0.0038304642
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0.137536094 0.0299827004 -0.0028256827 -0.0045674867 -0.0033860727
0.035502543 -0.0025510328 0.0123298802 -0.0019578378 -0.0012352890
0.182035183 -0.0024665186 -0.0023447736 0.0307302483 -0.0036859485
-0.880424689 0.0007957924 0.0001208034 -0.0046902190 0.0224426879
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-0.009313077 -0.1368368333 0.5915667707 -0.0550559425 -0.0256378945
0.001398727 -0.0948722569 -0.0550559425 0.4136545311 -0.0190373073
-0.041835607 -0.0455162475 -0.0256378945 -0.0190373073 0.2127275191
0.022911911 -0.2098486594 0.0340223545 0.0102161672 0.0084707499
0.010018870 0.0448232473 -0.2209108774 0.0148128614 0.0091130637
0.000369723 0.0086045805 0.0084271753 -0.0567556715 0.0015421246
-0.150771143 -0.0107823773 0.0218349479 -0.0202341089 -0.0554444513

-0.2410652748 1.558810e-02 0.0064294250 0.0956599413
0.0193520057 -1.594698e-01 0.0047529695 0.0485580295
0.0066595372 3.834239e-03 -0.0580203619 0.0187930166
0.0826913815 5.689408e-02 0.0137443694 -0.6037785259
-0.2126596733 2.177539e-02 0.0068771464 0.0232833502
0.0244478758 -2.191987e-01 0.0080217961 0.0353895251
0.0079935766 7.558007e-03 -0.0770320848 0.0107155495
0.0250158238 3.301493e-02 0.0089504876 -0.2959519775
-0.0233704312 5.290910e-03 0.0043979191 0.0087738144
0.0042014090 -2.827038e-02 0.0034858310 0.0088815411
0.0040343291 6.317681e-03 -0.0192634126 0.0052224958
0.0075599150 8.329953e-03 0.0053647356 -0.0372803569
-0.0448758614 3.964997e-03 0.0036783964 0.0320715476

```

0.0031110794 -2.942354e-02 0.0010115479 0.0065124972
0.0013684638 -1.360425e-04 -0.0196713847 0.0160335874
0.0311579694 1.521845e-02 0.0099557622 -0.0850446512
-0.1207222840 -3.257817e-03 0.0039660564 0.0904527985
0.0026072789 -1.475354e-02 -0.0011046065 0.0217234029
0.0064249566 -5.901417e-03 -0.0260597225 0.0220421477
0.0672738362 2.282151e-02 0.0142124521 -0.2803048232
-0.0171672177 4.771677e-04 0.0027903781 0.0070333176
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-0.0009057320 -7.631369e-05 -0.0345476832 0.0146601060
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0.0229119108 1.001887e-02 0.0003697230 -0.1507711428
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0.0340223545 -2.209109e-01 0.0084271753 0.0218349479
0.0102161672 1.481286e-02 -0.0567556715 -0.0202341089
0.0084707499 9.113064e-03 0.0015421246 -0.0554444513
0.6091206760 -5.884372e-02 -0.0232385607 -0.1394702478
-0.0588437212 4.417250e-01 -0.0167168738 -0.0900659188
-0.0232385607 -1.671687e-02 0.1894059794 -0.0427410709
-0.1394702478 -9.006592e-02 -0.0427410709 0.9062865924

```

\$dens

```

function (y)
sum(-lgamma(y + 1))
<environment: namespace:exactLoglinTest>

```

\$dobs

```
[1] 50.26369 52.56769
```

\$mu.hat

	75	74	73	72	70	69
1.31600087	0.48346172	0.18073692	6.51660315	1.13800295	0.81453108	
	68	67	60	59	58	57
0.25072319	1.60473559	0.18105409	0.13394981	0.26096632	0.21080481	
	55	54	53	52	50	49
1.97444067	0.52630855	1.21928164	6.54106633	5.63440188	2.92618991	
	48	47	40	39	38	37
5.58172191	5.31553870	0.13185304	0.07554443	0.51708045	0.55718074	
	35	34	33	32	30	29
0.79011836	0.16310491	1.32752883	9.50014868	1.78879234	0.71943767	
	28	27	20	19	18	17
4.82138891	6.12481782	1.78671996	1.50458067	0.82331031	0.24350239	
	80	79	78	77	76	71
1.03386967	1.05416634	0.33141537	1.79927933	5.78126929	5.50319734	
	66	65	64	63	62	61
8.19200719	2.51212650	0.64784087	0.23712452	10.07938194	13.52352617	
	56	51	46	45	44	43
0.21322497	1.73890282	8.54214760	2.21010335	0.41355173	0.93803014	
	42	41	36	31	26	25
5.93259017	2.50572461	0.71834133	3.21909922	12.54556326	0.28923627	
	24	23	22	21	16	15

0.04191298	0.33400181	2.81785276	1.51699618	4.64188666	6.78594333
14	13	12	11	10	9
2.05888356	1.33968017	2.63141457	13.18407836	1.30530606	0.77160008
8	7	6	5	4	3
0.41339354	0.14414063	4.36555969	3.12203064	0.66493568	0.42361598
2	1				
0.98094241	7.80847529				

\$n

[1] 80

\$n1

[1] 40

\$nosim

[1] 1000

\$s

	[,1]
(Intercept)	219
lake2	48
lake3	53
lake4	63
gender2	89
size2	95
food2	61
food3	19
food4	13
food5	32
lake2:food2	19
lake3:food2	18
lake4:food2	20
lake2:food3	7
lake3:food3	8
lake4:food3	1
lake2:food4	1
lake3:food4	4
lake4:food4	3
lake2:food5	3
lake3:food5	10
lake4:food5	6
gender2:food2	28
gender2:food3	6
gender2:food4	6
gender2:food5	14
size2:food2	16
size2:food3	13
size2:food4	8
size2:food5	13
lake2:gender2	17
lake3:gender2	13
lake4:gender2	24
lake2:size2	28
lake3:size2	29
lake4:size2	22
gender2:size2	22
lake2:gender2:size2	2
lake3:gender2:size2	1

```
lake4:gender2:size2 10
```

```
$stat
```

```
function (y = NULL, mu = NULL, rowlabels = FALSE)
```

```
{
```

```
  if (rowlabels)
```

```
    c("deviance", "Pearson")
```

```
  else {
```

```
    temp <- y != 0
```

```
    c(2 * sum(y[temp] * log(y[temp]/mu[temp])), sum((y -  
      mu)^2/mu))
```

```
  }
```

```
}
```

```
<environment: namespace:exactLoglinTest>
```

```
$tdf
```

```
[1] 3
```

```
$x
```

	(Intercept)	lake2	lake3	lake4	gender2	size2	food2	food3	food4	food5
75	1	0	0	1	1	0	0	0	0	1
74	1	0	0	1	1	0	0	0	1	0
73	1	0	0	1	1	0	0	1	0	0
72	1	0	0	1	1	0	1	0	0	0
70	1	0	0	1	0	1	0	0	0	1
69	1	0	0	1	0	1	0	0	1	0
68	1	0	0	1	0	1	0	1	0	0
67	1	0	0	1	0	1	1	0	0	0
60	1	0	1	0	1	1	0	0	0	1
59	1	0	1	0	1	1	0	0	1	0
58	1	0	1	0	1	1	0	1	0	0
57	1	0	1	0	1	1	1	0	0	0
55	1	0	1	0	1	0	0	0	0	1
54	1	0	1	0	1	0	0	0	1	0
53	1	0	1	0	1	0	0	1	0	0
52	1	0	1	0	1	0	1	0	0	0
50	1	0	1	0	0	1	0	0	0	1
49	1	0	1	0	0	1	0	0	1	0
48	1	0	1	0	0	1	0	1	0	0
47	1	0	1	0	0	1	1	0	0	0
40	1	1	0	0	1	1	0	0	0	1
39	1	1	0	0	1	1	0	0	1	0
38	1	1	0	0	1	1	0	1	0	0
37	1	1	0	0	1	1	1	0	0	0
35	1	1	0	0	1	0	0	0	0	1
34	1	1	0	0	1	0	0	0	1	0
33	1	1	0	0	1	0	0	1	0	0
32	1	1	0	0	1	0	1	0	0	0
30	1	1	0	0	0	1	0	0	0	1
29	1	1	0	0	0	1	0	0	1	0
28	1	1	0	0	0	1	0	1	0	0
27	1	1	0	0	0	1	1	0	0	0
20	1	0	0	0	1	1	0	0	0	1
19	1	0	0	0	1	1	0	0	1	0
18	1	0	0	0	1	1	0	1	0	0
17	1	0	0	0	1	1	1	0	0	0
80	1	0	0	1	1	1	0	0	0	1
79	1	0	0	1	1	1	0	0	1	0

78	1	0	0	1	1	1	0	1	0	0
77	1	0	0	1	1	1	1	0	0	0
76	1	0	0	1	1	1	0	0	0	0
71	1	0	0	1	1	0	0	0	0	0
66	1	0	0	1	0	1	0	0	0	0
65	1	0	0	1	0	0	0	0	0	1
64	1	0	0	1	0	0	0	0	1	0
63	1	0	0	1	0	0	0	1	0	0
62	1	0	0	1	0	0	1	0	0	0
61	1	0	0	1	0	0	0	0	0	0
56	1	0	1	0	1	1	0	0	0	0
51	1	0	1	0	1	0	0	0	0	0
46	1	0	1	0	0	1	0	0	0	0
45	1	0	1	0	0	0	0	0	0	1
44	1	0	1	0	0	0	0	0	1	0
43	1	0	1	0	0	0	0	1	0	0
42	1	0	1	0	0	0	1	0	0	0
41	1	0	1	0	0	0	0	0	0	0
36	1	1	0	0	1	1	0	0	0	0
31	1	1	0	0	1	0	0	0	0	0
26	1	1	0	0	0	1	0	0	0	0
25	1	1	0	0	0	0	0	0	0	1
24	1	1	0	0	0	0	0	0	1	0
23	1	1	0	0	0	0	0	1	0	0
22	1	1	0	0	0	0	1	0	0	0
21	1	1	0	0	0	0	0	0	0	0
16	1	0	0	0	1	1	0	0	0	0
15	1	0	0	0	1	0	0	0	0	1
14	1	0	0	0	1	0	0	0	1	0
13	1	0	0	0	1	0	0	1	0	0
12	1	0	0	0	1	0	1	0	0	0
11	1	0	0	0	1	0	0	0	0	0
10	1	0	0	0	0	1	0	0	0	1
9	1	0	0	0	0	1	0	0	1	0
8	1	0	0	0	0	1	0	1	0	0
7	1	0	0	0	0	1	1	0	0	0
6	1	0	0	0	0	1	0	0	0	0
5	1	0	0	0	0	0	0	0	0	1
4	1	0	0	0	0	0	0	0	1	0
3	1	0	0	0	0	0	0	1	0	0
2	1	0	0	0	0	0	1	0	0	0
1	1	0	0	0	0	0	0	0	0	0
	lake2:food2	lake3:food2	lake4:food2	lake2:food3	lake3:food3	lake4:food3				
75	0	0	0	0	0	0	0	0	0	
74	0	0	0	0	0	0	0	0	0	
73	0	0	0	0	0	0	0	0	1	
72	0	0	0	1	0	0	0	0	0	
70	0	0	0	0	0	0	0	0	0	
69	0	0	0	0	0	0	0	0	0	
68	0	0	0	0	0	0	0	0	1	
67	0	0	0	1	0	0	0	0	0	
60	0	0	0	0	0	0	0	0	0	
59	0	0	0	0	0	0	0	0	0	
58	0	0	0	0	0	0	1	0	0	
57	0	1	0	0	0	0	0	0	0	
55	0	0	0	0	0	0	0	0	0	
54	0	0	0	0	0	0	0	0	0	
53	0	0	0	0	0	1	0	0	0	

52	0	1	0	0	0	0
50	0	0	0	0	0	0
49	0	0	0	0	0	0
48	0	0	0	0	1	0
47	0	1	0	0	0	0
40	0	0	0	0	0	0
39	0	0	0	0	0	0
38	0	0	0	1	0	0
37	1	0	0	0	0	0
35	0	0	0	0	0	0
34	0	0	0	0	0	0
33	0	0	0	1	0	0
32	1	0	0	0	0	0
30	0	0	0	0	0	0
29	0	0	0	0	0	0
28	0	0	0	1	0	0
27	1	0	0	0	0	0
20	0	0	0	0	0	0
19	0	0	0	0	0	0
18	0	0	0	0	0	0
17	0	0	0	0	0	0
80	0	0	0	0	0	0
79	0	0	0	0	0	0
78	0	0	0	0	0	1
77	0	0	1	0	0	0
76	0	0	0	0	0	0
71	0	0	0	0	0	0
66	0	0	0	0	0	0
65	0	0	0	0	0	0
64	0	0	0	0	0	0
63	0	0	0	0	0	1
62	0	0	1	0	0	0
61	0	0	0	0	0	0
56	0	0	0	0	0	0
51	0	0	0	0	0	0
46	0	0	0	0	0	0
45	0	0	0	0	0	0
44	0	0	0	0	0	0
43	0	0	0	0	1	0
42	0	1	0	0	0	0
41	0	0	0	0	0	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	0	0	0
24	0	0	0	0	0	0
23	0	0	0	1	0	0
22	1	0	0	0	0	0
21	0	0	0	0	0	0
16	0	0	0	0	0	0
15	0	0	0	0	0	0
14	0	0	0	0	0	0
13	0	0	0	0	0	0
12	0	0	0	0	0	0
11	0	0	0	0	0	0
10	0	0	0	0	0	0
9	0	0	0	0	0	0
8	0	0	0	0	0	0

7	0	0	0	0	0	0
6	0	0	0	0	0	0
5	0	0	0	0	0	0
4	0	0	0	0	0	0
3	0	0	0	0	0	0
2	0	0	0	0	0	0
1	0	0	0	0	0	0
	lake2:food4	lake3:food4	lake4:food4	lake2:food5	lake3:food5	lake4:food5
75	0	0	0	0	0	1
74	0	0	1	0	0	0
73	0	0	0	0	0	0
72	0	0	0	0	0	0
70	0	0	0	0	0	1
69	0	0	1	0	0	0
68	0	0	0	0	0	0
67	0	0	0	0	0	0
60	0	0	0	0	1	0
59	0	1	0	0	0	0
58	0	0	0	0	0	0
57	0	0	0	0	0	0
55	0	0	0	0	1	0
54	0	1	0	0	0	0
53	0	0	0	0	0	0
52	0	0	0	0	0	0
50	0	0	0	0	1	0
49	0	1	0	0	0	0
48	0	0	0	0	0	0
47	0	0	0	0	0	0
40	0	0	0	1	0	0
39	1	0	0	0	0	0
38	0	0	0	0	0	0
37	0	0	0	0	0	0
35	0	0	0	1	0	0
34	1	0	0	0	0	0
33	0	0	0	0	0	0
32	0	0	0	0	0	0
30	0	0	0	1	0	0
29	1	0	0	0	0	0
28	0	0	0	0	0	0
27	0	0	0	0	0	0
20	0	0	0	0	0	0
19	0	0	0	0	0	0
18	0	0	0	0	0	0
17	0	0	0	0	0	0
80	0	0	0	0	0	1
79	0	0	1	0	0	0
78	0	0	0	0	0	0
77	0	0	0	0	0	0
76	0	0	0	0	0	0
71	0	0	0	0	0	0
66	0	0	0	0	0	0
65	0	0	0	0	0	1
64	0	0	1	0	0	0
63	0	0	0	0	0	0
62	0	0	0	0	0	0
61	0	0	0	0	0	0
56	0	0	0	0	0	0
51	0	0	0	0	0	0

46	0	0	0	0	0	0
45	0	0	0	0	1	0
44	0	1	0	0	0	0
43	0	0	0	0	0	0
42	0	0	0	0	0	0
41	0	0	0	0	0	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	1	0	0
24	1	0	0	0	0	0
23	0	0	0	0	0	0
22	0	0	0	0	0	0
21	0	0	0	0	0	0
16	0	0	0	0	0	0
15	0	0	0	0	0	0
14	0	0	0	0	0	0
13	0	0	0	0	0	0
12	0	0	0	0	0	0
11	0	0	0	0	0	0
10	0	0	0	0	0	0
9	0	0	0	0	0	0
8	0	0	0	0	0	0
7	0	0	0	0	0	0
6	0	0	0	0	0	0
5	0	0	0	0	0	0
4	0	0	0	0	0	0
3	0	0	0	0	0	0
2	0	0	0	0	0	0
1	0	0	0	0	0	0

	gender2:food2	gender2:food3	gender2:food4	gender2:food5	size2:food2
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75	0	0	0	1	0
74	0	0	1	0	0
73	0	1	0	0	0
72	1	0	0	0	0
70	0	0	0	0	0
69	0	0	0	0	0
68	0	0	0	0	0
67	0	0	0	0	1
60	0	0	0	1	0
59	0	0	1	0	0
58	0	1	0	0	0
57	1	0	0	0	1
55	0	0	0	1	0
54	0	0	1	0	0
53	0	1	0	0	0
52	1	0	0	0	0
50	0	0	0	0	0
49	0	0	0	0	0
48	0	0	0	0	0
47	0	0	0	0	1
40	0	0	0	1	0
39	0	0	1	0	0
38	0	1	0	0	0
37	1	0	0	0	1
35	0	0	0	1	0
34	0	0	1	0	0
33	0	1	0	0	0

32	1	0	0	0	0	0
30	0	0	0	0	0	0
29	0	0	0	0	0	0
28	0	0	0	0	0	0
27	0	0	0	0	0	1
20	0	0	0	0	1	0
19	0	0	1	0	0	0
18	0	1	0	0	0	0
17	1	0	0	0	0	1
80	0	0	0	0	1	0
79	0	0	1	0	0	0
78	0	1	0	0	0	0
77	1	0	0	0	0	1
76	0	0	0	0	0	0
71	0	0	0	0	0	0
66	0	0	0	0	0	0
65	0	0	0	0	0	0
64	0	0	0	0	0	0
63	0	0	0	0	0	0
62	0	0	0	0	0	0
61	0	0	0	0	0	0
56	0	0	0	0	0	0
51	0	0	0	0	0	0
46	0	0	0	0	0	0
45	0	0	0	0	0	0
44	0	0	0	0	0	0
43	0	0	0	0	0	0
42	0	0	0	0	0	0
41	0	0	0	0	0	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	0	0	0
24	0	0	0	0	0	0
23	0	0	0	0	0	0
22	0	0	0	0	0	0
21	0	0	0	0	0	0
16	0	0	0	0	0	0
15	0	0	0	0	1	0
14	0	0	1	0	0	0
13	0	1	0	0	0	0
12	1	0	0	0	0	0
11	0	0	0	0	0	0
10	0	0	0	0	0	0
9	0	0	0	0	0	0
8	0	0	0	0	0	0
7	0	0	0	0	0	1
6	0	0	0	0	0	0
5	0	0	0	0	0	0
4	0	0	0	0	0	0
3	0	0	0	0	0	0
2	0	0	0	0	0	0
1	0	0	0	0	0	0
	size2:food3	size2:food4	size2:food5	lake2:gender2	lake3:gender2	
75	0	0	0	0	0	
74	0	0	0	0	0	
73	0	0	0	0	0	
72	0	0	0	0	0	

70	0	0	1	0	0
69	0	1	0	0	0
68	1	0	0	0	0
67	0	0	0	0	0
60	0	0	1	0	1
59	0	1	0	0	1
58	1	0	0	0	1
57	0	0	0	0	1
55	0	0	0	0	1
54	0	0	0	0	1
53	0	0	0	0	1
52	0	0	0	0	1
50	0	0	1	0	0
49	0	1	0	0	0
48	1	0	0	0	0
47	0	0	0	0	0
40	0	0	1	1	0
39	0	1	0	1	0
38	1	0	0	1	0
37	0	0	0	1	0
35	0	0	0	1	0
34	0	0	0	1	0
33	0	0	0	1	0
32	0	0	0	1	0
30	0	0	1	0	0
29	0	1	0	0	0
28	1	0	0	0	0
27	0	0	0	0	0
20	0	0	1	0	0
19	0	1	0	0	0
18	1	0	0	0	0
17	0	0	0	0	0
80	0	0	1	0	0
79	0	1	0	0	0
78	1	0	0	0	0
77	0	0	0	0	0
76	0	0	0	0	0
71	0	0	0	0	0
66	0	0	0	0	0
65	0	0	0	0	0
64	0	0	0	0	0
63	0	0	0	0	0
62	0	0	0	0	0
61	0	0	0	0	0
56	0	0	0	0	1
51	0	0	0	0	1
46	0	0	0	0	0
45	0	0	0	0	0
44	0	0	0	0	0
43	0	0	0	0	0
42	0	0	0	0	0
41	0	0	0	0	0
36	0	0	0	1	0
31	0	0	0	1	0
26	0	0	0	0	0
25	0	0	0	0	0
24	0	0	0	0	0
23	0	0	0	0	0

22	0	0	0	0	0
21	0	0	0	0	0
16	0	0	0	0	0
15	0	0	0	0	0
14	0	0	0	0	0
13	0	0	0	0	0
12	0	0	0	0	0
11	0	0	0	0	0
10	0	0	1	0	0
9	0	1	0	0	0
8	1	0	0	0	0
7	0	0	0	0	0
6	0	0	0	0	0
5	0	0	0	0	0
4	0	0	0	0	0
3	0	0	0	0	0
2	0	0	0	0	0
1	0	0	0	0	0
	lake4:gender2	lake2:size2	lake3:size2	lake4:size2	gender2:size2
75	1	0	0	0	0
74	1	0	0	0	0
73	1	0	0	0	0
72	1	0	0	0	0
70	0	0	0	1	0
69	0	0	0	1	0
68	0	0	0	1	0
67	0	0	0	1	0
60	0	0	1	0	1
59	0	0	1	0	1
58	0	0	1	0	1
57	0	0	1	0	1
55	0	0	0	0	0
54	0	0	0	0	0
53	0	0	0	0	0
52	0	0	0	0	0
50	0	0	1	0	0
49	0	0	1	0	0
48	0	0	1	0	0
47	0	0	1	0	0
40	0	1	0	0	1
39	0	1	0	0	1
38	0	1	0	0	1
37	0	1	0	0	1
35	0	0	0	0	0
34	0	0	0	0	0
33	0	0	0	0	0
32	0	0	0	0	0
30	0	1	0	0	0
29	0	1	0	0	0
28	0	1	0	0	0
27	0	1	0	0	0
20	0	0	0	0	1
19	0	0	0	0	1
18	0	0	0	0	1
17	0	0	0	0	1
80	1	0	0	1	1
79	1	0	0	1	1
78	1	0	0	1	1

77	1	0	0	1	1
76	1	0	0	1	1
71	1	0	0	0	0
66	0	0	0	1	0
65	0	0	0	0	0
64	0	0	0	0	0
63	0	0	0	0	0
62	0	0	0	0	0
61	0	0	0	0	0
56	0	0	1	0	1
51	0	0	0	0	0
46	0	0	1	0	0
45	0	0	0	0	0
44	0	0	0	0	0
43	0	0	0	0	0
42	0	0	0	0	0
41	0	0	0	0	0
36	0	1	0	0	1
31	0	0	0	0	0
26	0	1	0	0	0
25	0	0	0	0	0
24	0	0	0	0	0
23	0	0	0	0	0
22	0	0	0	0	0
21	0	0	0	0	0
16	0	0	0	0	1
15	0	0	0	0	0
14	0	0	0	0	0
13	0	0	0	0	0
12	0	0	0	0	0
11	0	0	0	0	0
10	0	0	0	0	0
9	0	0	0	0	0
8	0	0	0	0	0
7	0	0	0	0	0
6	0	0	0	0	0
5	0	0	0	0	0
4	0	0	0	0	0
3	0	0	0	0	0
2	0	0	0	0	0
1	0	0	0	0	0

lake2:gender2:size2 lake3:gender2:size2 lake4:gender2:size2

75	0	0	0
74	0	0	0
73	0	0	0
72	0	0	0
70	0	0	0
69	0	0	0
68	0	0	0
67	0	0	0
60	0	1	0
59	0	1	0
58	0	1	0
57	0	1	0
55	0	0	0
54	0	0	0
53	0	0	0
52	0	0	0

50	0	0	0
49	0	0	0
48	0	0	0
47	0	0	0
40	1	0	0
39	1	0	0
38	1	0	0
37	1	0	0
35	0	0	0
34	0	0	0
33	0	0	0
32	0	0	0
30	0	0	0
29	0	0	0
28	0	0	0
27	0	0	0
20	0	0	0
19	0	0	0
18	0	0	0
17	0	0	0
80	0	0	1
79	0	0	1
78	0	0	1
77	0	0	1
76	0	0	1
71	0	0	0
66	0	0	0
65	0	0	0
64	0	0	0
63	0	0	0
62	0	0	0
61	0	0	0
56	0	1	0
51	0	0	0
46	0	0	0
45	0	0	0
44	0	0	0
43	0	0	0
42	0	0	0
41	0	0	0
36	1	0	0
31	0	0	0
26	0	0	0
25	0	0	0
24	0	0	0
23	0	0	0
22	0	0	0
21	0	0	0
16	0	0	0
15	0	0	0
14	0	0	0
13	0	0	0
12	0	0	0
11	0	0	0
10	0	0	0
9	0	0	0
8	0	0	0
7	0	0	0

6	0	0	0
5	0	0	0
4	0	0	0
3	0	0	0
2	0	0	0
1	0	0	0

\$x1

	(Intercept)	lake2	lake3	lake4	gender2	size2	food2	food3	food4	food5
75	1	0	0	1	1	0	0	0	0	1
74	1	0	0	1	1	0	0	0	1	0
73	1	0	0	1	1	0	0	1	0	0
72	1	0	0	1	1	0	1	0	0	0
70	1	0	0	1	0	1	0	0	0	1
69	1	0	0	1	0	1	0	0	1	0
68	1	0	0	1	0	1	0	1	0	0
67	1	0	0	1	0	1	1	0	0	0
60	1	0	1	0	1	1	0	0	0	1
59	1	0	1	0	1	1	0	0	1	0
58	1	0	1	0	1	1	0	1	0	0
57	1	0	1	0	1	1	1	0	0	0
55	1	0	1	0	1	0	0	0	0	1
54	1	0	1	0	1	0	0	0	1	0
53	1	0	1	0	1	0	0	1	0	0
52	1	0	1	0	1	0	1	0	0	0
50	1	0	1	0	0	1	0	0	0	1
49	1	0	1	0	0	1	0	0	1	0
48	1	0	1	0	0	1	0	1	0	0
47	1	0	1	0	0	1	1	0	0	0
40	1	1	0	0	1	1	0	0	0	1
39	1	1	0	0	1	1	0	0	1	0
38	1	1	0	0	1	1	0	1	0	0
37	1	1	0	0	1	1	1	0	0	0
35	1	1	0	0	1	0	0	0	0	1
34	1	1	0	0	1	0	0	0	1	0
33	1	1	0	0	1	0	0	1	0	0
32	1	1	0	0	1	0	1	0	0	0
30	1	1	0	0	0	1	0	0	0	1
29	1	1	0	0	0	1	0	0	1	0
28	1	1	0	0	0	1	0	1	0	0
27	1	1	0	0	0	1	1	0	0	0
20	1	0	0	0	1	1	0	0	0	1
19	1	0	0	0	1	1	0	0	1	0
18	1	0	0	0	1	1	0	1	0	0
17	1	0	0	0	1	1	1	0	0	0
80	1	0	0	1	1	1	0	0	0	1
79	1	0	0	1	1	1	0	0	1	0
78	1	0	0	1	1	1	0	1	0	0
77	1	0	0	1	1	1	1	0	0	0
	lake2:food2	lake3:food2	lake4:food2	lake2:food3	lake3:food3	lake4:food3				
75	0	0	0	0	0	0				0
74	0	0	0	0	0	0				0
73	0	0	0	0	0	0				1
72	0	0	0	1	0	0				0
70	0	0	0	0	0	0				0
69	0	0	0	0	0	0				0
68	0	0	0	0	0	0				1
67	0	0	0	1	0	0				0

60	0	0	0	0	0	0
59	0	0	0	0	0	0
58	0	0	0	0	1	0
57	0	1	0	0	0	0
55	0	0	0	0	0	0
54	0	0	0	0	0	0
53	0	0	0	0	1	0
52	0	1	0	0	0	0
50	0	0	0	0	0	0
49	0	0	0	0	0	0
48	0	0	0	0	1	0
47	0	1	0	0	0	0
40	0	0	0	0	0	0
39	0	0	0	0	0	0
38	0	0	0	1	0	0
37	1	0	0	0	0	0
35	0	0	0	0	0	0
34	0	0	0	0	0	0
33	0	0	0	1	0	0
32	1	0	0	0	0	0
30	0	0	0	0	0	0
29	0	0	0	0	0	0
28	0	0	0	1	0	0
27	1	0	0	0	0	0
20	0	0	0	0	0	0
19	0	0	0	0	0	0
18	0	0	0	0	0	0
17	0	0	0	0	0	0
80	0	0	0	0	0	0
79	0	0	0	0	0	0
78	0	0	0	0	0	1
77	0	0	1	0	0	0
	lake2:food4	lake3:food4	lake4:food4	lake2:food5	lake3:food5	lake4:food5
75	0	0	0	0	0	1
74	0	0	1	0	0	0
73	0	0	0	0	0	0
72	0	0	0	0	0	0
70	0	0	0	0	0	1
69	0	0	1	0	0	0
68	0	0	0	0	0	0
67	0	0	0	0	0	0
60	0	0	0	0	1	0
59	0	1	0	0	0	0
58	0	0	0	0	0	0
57	0	0	0	0	0	0
55	0	0	0	0	1	0
54	0	1	0	0	0	0
53	0	0	0	0	0	0
52	0	0	0	0	0	0
50	0	0	0	0	1	0
49	0	1	0	0	0	0
48	0	0	0	0	0	0
47	0	0	0	0	0	0
40	0	0	0	1	0	0
39	1	0	0	0	0	0
38	0	0	0	0	0	0
37	0	0	0	0	0	0
35	0	0	0	1	0	0

34	1	0	0	0	0	0	0
33	0	0	0	0	0	0	0
32	0	0	0	0	0	0	0
30	0	0	0	1	0	0	0
29	1	0	0	0	0	0	0
28	0	0	0	0	0	0	0
27	0	0	0	0	0	0	0
20	0	0	0	0	0	0	0
19	0	0	0	0	0	0	0
18	0	0	0	0	0	0	0
17	0	0	0	0	0	0	0
80	0	0	0	0	0	0	1
79	0	0	1	0	0	0	0
78	0	0	0	0	0	0	0
77	0	0	0	0	0	0	0

	gender2:food2	gender2:food3	gender2:food4	gender2:food5	size2:food2	
75	0	0	0	1	0	
74	0	0	1	0	0	
73	0	1	0	0	0	
72	1	0	0	0	0	
70	0	0	0	0	0	
69	0	0	0	0	0	
68	0	0	0	0	0	
67	0	0	0	0	1	
60	0	0	0	1	0	
59	0	0	1	0	0	
58	0	1	0	0	0	
57	1	0	0	0	1	
55	0	0	0	1	0	
54	0	0	1	0	0	
53	0	1	0	0	0	
52	1	0	0	0	0	
50	0	0	0	0	0	
49	0	0	0	0	0	
48	0	0	0	0	0	
47	0	0	0	0	1	
40	0	0	0	1	0	
39	0	0	1	0	0	
38	0	1	0	0	0	
37	1	0	0	0	1	
35	0	0	0	1	0	
34	0	0	1	0	0	
33	0	1	0	0	0	
32	1	0	0	0	0	
30	0	0	0	0	0	
29	0	0	0	0	0	
28	0	0	0	0	0	
27	0	0	0	0	1	
20	0	0	0	1	0	
19	0	0	1	0	0	
18	0	1	0	0	0	
17	1	0	0	0	1	
80	0	0	0	1	0	
79	0	0	1	0	0	
78	0	1	0	0	0	
77	1	0	0	0	1	

	size2:food3	size2:food4	size2:food5	lake2:gender2	lake3:gender2
75	0	0	0	0	0

74	0	0	0	0	0
73	0	0	0	0	0
72	0	0	0	0	0
70	0	0	1	0	0
69	0	1	0	0	0
68	1	0	0	0	0
67	0	0	0	0	0
60	0	0	1	0	1
59	0	1	0	0	1
58	1	0	0	0	1
57	0	0	0	0	1
55	0	0	0	0	1
54	0	0	0	0	1
53	0	0	0	0	1
52	0	0	0	0	1
50	0	0	1	0	0
49	0	1	0	0	0
48	1	0	0	0	0
47	0	0	0	0	0
40	0	0	1	1	0
39	0	1	0	1	0
38	1	0	0	1	0
37	0	0	0	1	0
35	0	0	0	1	0
34	0	0	0	1	0
33	0	0	0	1	0
32	0	0	0	1	0
30	0	0	1	0	0
29	0	1	0	0	0
28	1	0	0	0	0
27	0	0	0	0	0
20	0	0	1	0	0
19	0	1	0	0	0
18	1	0	0	0	0
17	0	0	0	0	0
80	0	0	1	0	0
79	0	1	0	0	0
78	1	0	0	0	0
77	0	0	0	0	0
lake4:gender2	lake2:size2	lake3:size2	lake4:size2	gender2:size2	
75	1	0	0	0	0
74	1	0	0	0	0
73	1	0	0	0	0
72	1	0	0	0	0
70	0	0	0	1	0
69	0	0	0	1	0
68	0	0	0	1	0
67	0	0	0	1	0
60	0	0	1	0	1
59	0	0	1	0	1
58	0	0	1	0	1
57	0	0	1	0	1
55	0	0	0	0	0
54	0	0	0	0	0
53	0	0	0	0	0
52	0	0	0	0	0
50	0	0	1	0	0
49	0	0	1	0	0

48	0	0	1	0	0
47	0	0	1	0	0
40	0	1	0	0	1
39	0	1	0	0	1
38	0	1	0	0	1
37	0	1	0	0	1
35	0	0	0	0	0
34	0	0	0	0	0
33	0	0	0	0	0
32	0	0	0	0	0
30	0	1	0	0	0
29	0	1	0	0	0
28	0	1	0	0	0
27	0	1	0	0	0
20	0	0	0	0	1
19	0	0	0	0	1
18	0	0	0	0	1
17	0	0	0	0	1
80	1	0	0	1	1
79	1	0	0	1	1
78	1	0	0	1	1
77	1	0	0	1	1

lake2:gender2:size2 lake3:gender2:size2 lake4:gender2:size2

75	0	0	0
74	0	0	0
73	0	0	0
72	0	0	0
70	0	0	0
69	0	0	0
68	0	0	0
67	0	0	0
60	0	1	0
59	0	1	0
58	0	1	0
57	0	1	0
55	0	0	0
54	0	0	0
53	0	0	0
52	0	0	0
50	0	0	0
49	0	0	0
48	0	0	0
47	0	0	0
40	1	0	0
39	1	0	0
38	1	0	0
37	1	0	0
35	0	0	0
34	0	0	0
33	0	0	0
32	0	0	0
30	0	0	0
29	0	0	0
28	0	0	0
27	0	0	0
20	0	0	0
19	0	0	0
18	0	0	0

17	0	0	0
80	0	0	1
79	0	0	1
78	0	0	1
77	0	0	1

\$x2invt

	(Intercept)	lake2	lake3	lake4	gender2	size2	food2	food3	food4	food5
76	0	0	0	0	0	0	0	0	0	0
71	0	0	0	0	0	0	0	0	0	0
66	0	0	0	0	0	0	0	0	0	0
65	0	0	0	0	0	0	0	0	0	0
64	0	0	0	0	0	0	0	0	0	0
63	0	0	0	0	0	0	0	0	0	0
62	0	0	0	0	0	0	0	0	0	0
61	0	0	0	1	0	0	0	0	0	0
56	0	0	0	0	0	0	0	0	0	0
51	0	0	0	0	0	0	0	0	0	0
46	0	0	0	0	0	0	0	0	0	0
45	0	0	0	0	0	0	0	0	0	0
44	0	0	0	0	0	0	0	0	0	0
43	0	0	0	0	0	0	0	0	0	0
42	0	0	0	0	0	0	0	0	0	0
41	0	0	1	0	0	0	0	0	0	0
36	0	0	0	0	0	0	0	0	0	0
31	0	0	0	0	0	0	0	0	0	0
26	0	0	0	0	0	0	0	0	0	0
25	0	0	0	0	0	0	0	0	0	0
24	0	0	0	0	0	0	0	0	0	0
23	0	0	0	0	0	0	0	0	0	0
22	0	0	0	0	0	0	0	0	0	0
21	0	1	0	0	0	0	0	0	0	0
16	0	0	0	0	0	0	0	0	0	0
15	0	0	0	0	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0
13	0	0	0	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0
11	0	0	0	0	1	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	1	0	0	0	0
5	0	0	0	0	0	0	0	0	0	1
4	0	0	0	0	0	0	0	1	0	0
3	0	0	0	0	0	0	1	0	0	0
2	0	0	0	0	0	0	1	0	0	0
1	1	-1	-1	-1	-1	-1	-1	-1	-1	-1
	lake2:food2	lake3:food2	lake4:food2	lake2:food3	lake3:food3	lake4:food3				
76	0	0	0	0	0	0	0	0	0	0
71	0	0	0	0	0	0	0	0	0	0
66	0	0	0	0	0	0	0	0	0	0
65	0	0	0	0	0	0	0	0	0	0
64	0	0	0	0	0	0	0	0	0	0
63	0	0	0	0	0	0	0	0	1	0
62	0	0	0	1	0	0	0	0	0	0
61	0	0	0	-1	0	0	0	0	-1	0
56	0	0	0	0	0	0	0	0	0	0

51	0	0	0	0	0	0
46	0	0	0	0	0	0
45	0	0	0	0	0	0
44	0	0	0	0	0	0
43	0	0	0	0	1	0
42	0	1	0	0	0	0
41	0	-1	0	0	-1	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	0	0	0
24	0	0	0	0	0	0
23	0	0	0	1	0	0
22	1	0	0	0	0	0
21	-1	0	0	-1	0	0
16	0	0	0	0	0	0
15	0	0	0	0	0	0
14	0	0	0	0	0	0
13	0	0	0	0	0	0
12	0	0	0	0	0	0
11	0	0	0	0	0	0
10	0	0	0	0	0	0
9	0	0	0	0	0	0
8	0	0	0	0	0	0
7	0	0	0	0	0	0
6	0	0	0	0	0	0
5	0	0	0	0	0	0
4	0	0	0	0	0	0
3	0	0	0	-1	-1	-1
2	-1	-1	-1	0	0	0
1	1	1	1	1	1	1
	lake2:food4	lake3:food4	lake4:food4	lake2:food5	lake3:food5	lake4:food5
76	0	0	0	0	0	0
71	0	0	0	0	0	0
66	0	0	0	0	0	0
65	0	0	0	0	0	1
64	0	0	1	0	0	0
63	0	0	0	0	0	0
62	0	0	0	0	0	0
61	0	0	-1	0	0	-1
56	0	0	0	0	0	0
51	0	0	0	0	0	0
46	0	0	0	0	0	0
45	0	0	0	0	1	0
44	0	1	0	0	0	0
43	0	0	0	0	0	0
42	0	0	0	0	0	0
41	0	-1	0	0	-1	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	1	0	0
24	1	0	0	0	0	0
23	0	0	0	0	0	0
22	0	0	0	0	0	0
21	-1	0	0	-1	0	0
16	0	0	0	0	0	0
15	0	0	0	0	0	0

14	0	0	0	0	0	0	0
13	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0
11	0	0	0	0	0	0	0
10	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0
8	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0
5	0	0	0	-1	-1	-1	-1
4	-1	-1	-1	0	0	0	0
3	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0
1	1	1	1	1	1	1	1

	gender2:food2	gender2:food3	gender2:food4	gender2:food5	size2:food2	
76	0	0	0	0	0	0
71	0	0	0	0	0	0
66	0	0	0	0	0	0
65	0	0	0	0	0	0
64	0	0	0	0	0	0
63	0	0	0	0	0	0
62	0	0	0	0	0	0
61	0	0	0	0	0	0
56	0	0	0	0	0	0
51	0	0	0	0	0	0
46	0	0	0	0	0	0
45	0	0	0	0	0	0
44	0	0	0	0	0	0
43	0	0	0	0	0	0
42	0	0	0	0	0	0
41	0	0	0	0	0	0
36	0	0	0	0	0	0
31	0	0	0	0	0	0
26	0	0	0	0	0	0
25	0	0	0	0	0	0
24	0	0	0	0	0	0
23	0	0	0	0	0	0
22	0	0	0	0	0	0
21	0	0	0	0	0	0
16	0	0	0	0	0	0
15	0	0	0	1	0	0
14	0	0	1	0	0	0
13	0	1	0	0	0	0
12	1	0	0	0	0	0
11	-1	-1	-1	-1	-1	0
10	0	0	0	0	0	0
9	0	0	0	0	0	0
8	0	0	0	0	0	0
7	0	0	0	0	0	1
6	0	0	0	0	0	-1
5	0	0	0	-1	0	0
4	0	0	-1	0	0	0
3	0	-1	0	0	0	0
2	-1	0	0	0	0	-1
1	1	1	1	1	1	1

	size2:food3	size2:food4	size2:food5	lake2:gender2	lake3:gender2	
76	0	0	0	0	0	0
71	0	0	0	0	0	0

66	0	0	0	0	0
65	0	0	0	0	0
64	0	0	0	0	0
63	0	0	0	0	0
62	0	0	0	0	0
61	0	0	0	0	0
56	0	0	0	0	0
51	0	0	0	0	1
46	0	0	0	0	0
45	0	0	0	0	0
44	0	0	0	0	0
43	0	0	0	0	0
42	0	0	0	0	0
41	0	0	0	0	-1
36	0	0	0	0	0
31	0	0	0	1	0
26	0	0	0	0	0
25	0	0	0	0	0
24	0	0	0	0	0
23	0	0	0	0	0
22	0	0	0	0	0
21	0	0	0	-1	0
16	0	0	0	0	0
15	0	0	0	0	0
14	0	0	0	0	0
13	0	0	0	0	0
12	0	0	0	0	0
11	0	0	0	-1	-1
10	0	0	1	0	0
9	0	1	0	0	0
8	1	0	0	0	0
7	0	0	0	0	0
6	-1	-1	-1	0	0
5	0	0	-1	0	0
4	0	-1	0	0	0
3	-1	0	0	0	0
2	0	0	0	0	0
1	1	1	1	1	1
	lake4:gender2	lake2:size2	lake3:size2	lake4:size2	gender2:size2
76	0	0	0	0	0
71	1	0	0	0	0
66	0	0	0	1	0
65	0	0	0	0	0
64	0	0	0	0	0
63	0	0	0	0	0
62	0	0	0	0	0
61	-1	0	0	-1	0
56	0	0	0	0	0
51	0	0	0	0	0
46	0	0	1	0	0
45	0	0	0	0	0
44	0	0	0	0	0
43	0	0	0	0	0
42	0	0	0	0	0
41	0	0	-1	0	0
36	0	0	0	0	0
31	0	0	0	0	0
26	0	1	0	0	0

25	0	0	0	0	0
24	0	0	0	0	0
23	0	0	0	0	0
22	0	0	0	0	0
21	0	-1	0	0	0
16	0	0	0	0	1
15	0	0	0	0	0
14	0	0	0	0	0
13	0	0	0	0	0
12	0	0	0	0	0
11	-1	0	0	0	-1
10	0	0	0	0	0
9	0	0	0	0	0
8	0	0	0	0	0
7	0	0	0	0	0
6	0	-1	-1	-1	-1
5	0	0	0	0	0
4	0	0	0	0	0
3	0	0	0	0	0
2	0	0	0	0	0
1	1	1	1	1	1

lake2:gender2:size2 lake3:gender2:size2 lake4:gender2:size2

76	0	0	1
71	0	0	-1
66	0	0	-1
65	0	0	0
64	0	0	0
63	0	0	0
62	0	0	0
61	0	0	1
56	0	1	0
51	0	-1	0
46	0	-1	0
45	0	0	0
44	0	0	0
43	0	0	0
42	0	0	0
41	0	1	0
36	1	0	0
31	-1	0	0
26	-1	0	0
25	0	0	0
24	0	0	0
23	0	0	0
22	0	0	0
21	1	0	0
16	-1	-1	-1
15	0	0	0
14	0	0	0
13	0	0	0
12	0	0	0
11	1	1	1
10	0	0	0
9	0	0	0
8	0	0	0
7	0	0	0
6	1	1	1
5	0	0	0


```

4           0           0           0
3           0           0           0
2           0           0           0
1          -1          -1          -1

```

\$y

```

75 74 73 72 70 69 68 67 60 59 58 57 55 54 53 52 50 49 48 47 40 39 38 37 35 34
 1  0  1  9  2  1  0  0  0  0  0  1  4  1  1  4  5  3  6  6  0  1  0  1  2  0
33 32 30 29 28 27 20 19 18 17 80 79 78 77 76 71 66 65 64 63 62 61 56 51 46 45
 1  9  0  0  6  7  3  2  1  0  1  0  0  1  8  3  9  2  2  0 10 13  0  2  8  1
44 43 42 41 36 31 26 25 24 23 22 21 16 15 14 13 12 11 10  9  8  7  6  5  4  3
 0  1  7  3  0  3 13  1  0  0  2  2  3  3  2  2  3 16  2  1  0  0  4  5  0  0
 2  1
 1  7

```

\$ord

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[1] 75 74 73 72 70 69 68 67 60 59 58 57 55 54 53 52 50 49 48 47 40 39 38 37 35
[26] 34 33 32 30 29 28 27 20 19 18 17 80 79 78 77 76 71 66 65 64 63 62 61 56 51
[51] 46 45 44 43 42 41 36 31 26 25 24 23 22 21 16 15 14 13 12 11 10  9  8  7  6
[76]  5  4  3  2  1

```

\$glm.fit

Call: glm(formula = formula, family = poisson, data = data, x = TRUE, y = TRUE)

Coefficients:

(Intercept)	lake2	lake3
2.05521	-1.63848	-1.13663
lake4	gender2	size2
0.54922	0.52380	-0.58146
food2	food3	food4
-2.07445	-2.91414	-2.46327
food5	lake2:food2	lake3:food2
-0.91673	2.69369	2.93633
lake4:food2	lake2:food3	lake3:food3
1.78051	1.40080	1.93159
lake4:food3	lake2:food4	lake3:food4
-1.12946	-1.12562	0.66172
lake4:food4	lake2:food5	lake3:food5
-0.57527	-0.74052	0.79119
lake4:food5	gender2:food2	gender2:food3
-0.76658	0.46296	0.62756
gender2:food4	gender2:food5	size2:food2
0.60643	0.25257	-1.33626
size2:food3	size2:food4	size2:food5
0.55704	0.73024	-0.29058
lake2:gender2	lake3:gender2	lake4:gender2
0.22857	-0.88912	-1.42290
lake2:size2	lake3:size2	lake4:size2
2.69410	1.80790	0.08019
gender2:size2	lake2:gender2:size2	lake3:gender2:size2
-0.46243	-3.15012	-2.86267
lake4:gender2:size2		
1.01299		

Degrees of Freedom: 79 Total (i.e. Null); 40 Residual
Null Deviance: 307.2

Residual Deviance: 50.26

AIC: 293.7

\$p

[1] 0.4

\$batchsize

[1] 100

\$startiter

[1] 1001

\$mhap

[1] 5

\$chain

	deviance	Pearson
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[965,] 38.35763 37.72696
[966,] 38.35763 37.72696
[967,] 38.35763 37.72696
[968,] 38.35763 37.72696
[969,] 38.35763 37.72696
[970,] 38.35763 37.72696

```

[971,] 38.35763 37.72696
[972,] 38.35763 37.72696
[973,] 38.35763 37.72696
[974,] 38.35763 37.72696
[975,] 38.35763 37.72696
[976,] 38.35763 37.72696
[977,] 38.35763 37.72696
[978,] 38.35763 37.72696
[979,] 38.35763 37.72696
[980,] 38.35763 37.72696
[981,] 38.35763 37.72696
[982,] 38.35763 37.72696
[983,] 38.35763 37.72696
[984,] 38.35763 37.72696
[985,] 38.35763 37.72696
[986,] 38.35763 37.72696
[987,] 38.35763 37.72696
[988,] 38.35763 37.72696
[989,] 38.35763 37.72696
[990,] 38.35763 37.72696
[991,] 38.35763 37.72696
[992,] 38.35763 37.72696
[993,] 38.35763 37.72696
[994,] 38.35763 37.72696
[995,] 38.35763 37.72696
[996,] 38.35763 37.72696
[997,] 38.35763 37.72696
[998,] 38.35763 37.72696
[999,] 38.35763 37.72696
[1000,] 38.35763 37.72696

```

```

$current.batchmean
[1] 0 0

```

```

$bmsq
[1] 2.1117 2.1117

```

```

$nobatches
[1] 10

```

```

$phat
[1] 0.251 0.251

```

```

$mcse
[1] 0.1217247 0.1217247

```

```

$y1.start
[1] 0 0 0 8 2 1 0 1 0 0 0 0 2 0 1 7 5 4 6 4 0 0 1 1 1 0 1 9 1 1 5 6 3 0 2 0 1 2
[39] 0 3

```

```

$perpos
[1] 0.02

```

```

attr(,"class")
[1] "cabSummary"

```

The chain of goodness of fit statistics are saved in `alligator.mcx$chain`. The saved chain is discarded if the simulations are resumed with `update`, even if `savechain = T` when the simulation is resumed.

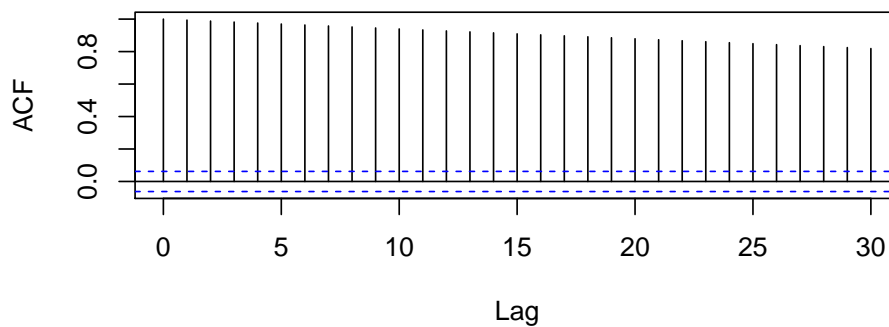
We would want to look at the autocorrelation function of the goodness of fit statistics.

```

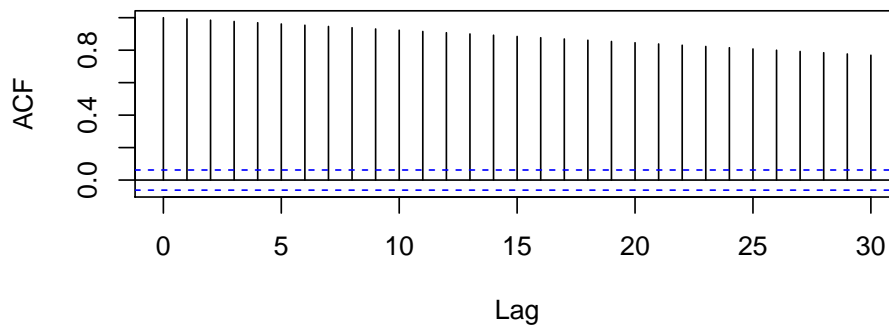
> par(mfrow = c(2, 1))
> acf(alligator.mcx$chain[,1])
> acf(alligator.mcx$chain[,2])

```

Series alligator.mcx\$chain[, 1]



Series alligator.mcx\$chain[, 2]



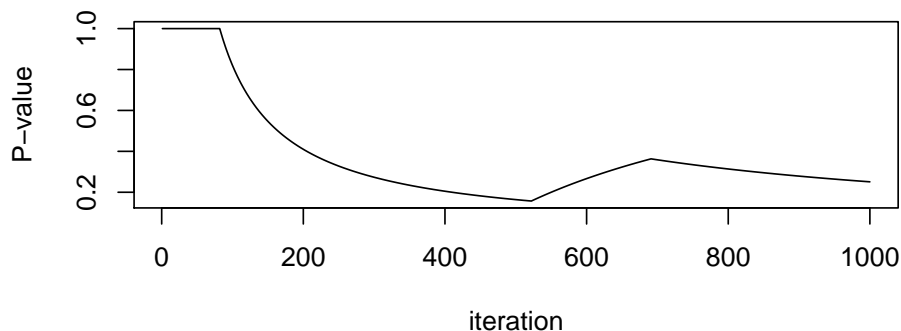
We would also want to look at the chain of P-values.

```

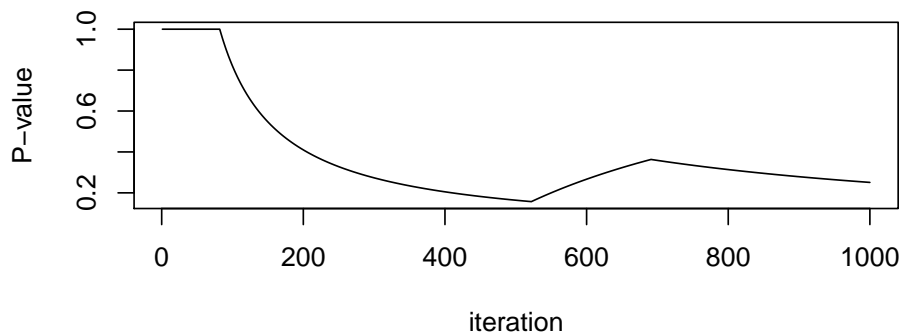
> dev.p <- cumsum(alligator.mcx$chain[,1] >= alligator.mcx$dobs[1]) / (1 : alligator.mcx$nosim)
> pearson.p <- cumsum(alligator.mcx$chain[,1] >= alligator.mcx$dobs[1]) / (1 : alligator.mcx$nosim)
> par(mfrow = c(2, 1))
> plot(dev.p, type = "l", ylab = "P-value", xlab = "iteration")
> title("Deviance P-value by iteration")
> plot(pearson.p, type = "l", ylab = "P-value", xlab = "iteration")
> title("Pearson P-value by iteration")

```

Deviance P-value by iteration



Pearson P-value by iteration



The P-values have apparently not stabilized. Also, there is an extremely slow decay in the autocorrelations of the chain of goodness of fit statistics. Therefore, we should execute a longer run using large batch sizes. While on the subject of batch sizes, note that `mcexact` does not require the total number of simulations to be a multiple of the batch size. If the algorithm terminates in the middle of completing a batch, it is not used in the P-value calculations. However, the simulations are not wasted if the algorithm is resumed with `update`.

One large final run of this data discarding all of the initial tinkering could be performed by setting `flush = TRUE` as an argument to `update`. Here, `flush = TRUE`, tells `update` to throw out all of the data used in the initial tinkering, except that it starts the new chain from the final table from the initial runs. This is a harmless way to burn the chain in while you are tinkering with it. Of course, the chain can be restarted at the default starting value, the observed data, by simply rerunning `mcexact`.

4 Application to Disclosure Limitation

Though there are certainly more rigorous procedures available [see 4], `exactLoglinTest` is a useful tool for exploring disclosure limitation in contingency tables. Consider the Czech Auto Worker's data given in Table 4. Suppose a researcher is concerned about the potential disclosure risk of releasing all two-way marginals from this table. The following code will load the Czech auto worker data into a data frame:

```
> data(czech.dat)
```

We will explore disclosure limitation by simulating tables from the hypergeometric distribution obtained by conditioning on all two way margins. However, we would like to save all of the simulated table entries, not just the deviance and Pearson statistics. This could be accomplished by changing the argument `stat` of `mcexact` to an appropriate statistic. However, the function `simulateConditional` performs this simulation for us. It returns the simulated tables in a matrix with each row being a complete simulated table.

Now we run the chain. Notice the `stat = cell.stat` option to load the newly defined statistic.

```

> chain <- simulateConditional(y ~ (A + B + C + D + E + F) ^ 2,
+                               data = czech.dat,
+                               method = "cab",
+                               nosim = 10 ^ 3,
+                               p = .4)

```

Now, `chain` is a matrix where each row is a simulated table. We were particularly concerned with cells 39, 48, and 55 which contained only one, two and two individuals respectively. Consider the proportion of tables which have greater than 0 but fewer than three individuals

```

> mean(chain[,39] > 0 & chain[,39] < 3)

```

```

[1] 0.389

```

```

> mean(chain[,48] > 0 & chain[,58] < 3)

```

```

[1] 0.11

```

```

> mean(chain[,55] > 0 & chain[,55] < 3)

```

```

[1] 0.896

```

We used the model in question because this model fixes all two-way margins. However, that model need not fit the data well (in fact, it doesn't). Therefore, in addition to simulating from the hypergeometric density, a user would likely also want to simulate from other densities, such as a uniform distribution on tables with these margins. Though the normal approximations for `exactLoglinTest` were tailored specifically to the hypergeometric density, it allows for other target distributions. Here the density must be specified on the log scale up to a constant. Since a uniform density is simply a constant we use a density that always returns 0.

```

> chain2 <- simulateConditional(y ~ (A + B + C + D + E + F) ^ 2,
+                               data = czech.dat,
+                               method = "cab",
+                               nosim = 10 ^ 3,
+                               p = .4,
+                               dens = function(y) 0)
> mean(chain2[,39] > 0 & chain2[,39] < 3)

```

```

[1] 0.363

```

```

> mean(chain2[,48] > 0 & chain2[,58] < 3)

```

```

[1] 0.59

```

```

> mean(chain2[,55] > 0 & chain2[,55] < 3)

```

```

[1] 1

```

Both simulations suggest that there are plenty of tables with higher counts than the observed counts for cells 39, 48 and 55. Hence the disclosure risk in releasing the two-way marginals seems minimal. However, it should be reiterated that this example is given only to illustrate how to obtain simulated tables from `exactLoglinTest`, further investigation of the chain and the data would be necessary for a thorough analysis of the disclosure risk.

4.1 Exact Score Test for Binomial Counts

The data given in A are obtained from the Cytel web site¹. The data cross classify the survival of the Titanic passengers by class, gender and age. You can obtain the data with

```

> data(titanic.dat)

```

¹<http://www.cytel.com/>

Following the analysis done at the Cytel web site, we view each person's survival as a binary outcome. We use a model where a person's age, sex and class are additive effects on the logit scale. In the light of the discussion from Subsection 1.1, this model is equivalent to the following:

```
> titanic.dat$alpha <- rep(1 : 16, 2)
> fit <- glm(y ~ (factor(class) + factor(age) + factor(sex)) : factor(surv) +
+           factor(surv) + factor(alpha),
+           family = poisson,
+           data = titanic.dat)
> summary(fit)
```

Call:

```
glm(formula = y ~ (factor(class) + factor(age) + factor(sex)):factor(surv) +
    factor(surv) + factor(alpha), family = poisson, data = titanic.dat)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-3.7995	-1.7072	-0.0003	0.9135	3.5931

Coefficients: (5 not defined because of singularities)

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-18.7133	2170.2682	-0.009	0.993
factor(surv)1	2.2477	0.2988	7.522	5.40e-14 ***
factor(alpha)2	16.4218	2170.2684	0.008	0.994
factor(alpha)3	18.9137	2170.2682	0.009	0.993
factor(alpha)4	19.6645	2170.2682	0.009	0.993
factor(alpha)5	19.3346	2170.2682	0.009	0.993
factor(alpha)6	21.3136	2170.2682	0.010	0.992
factor(alpha)7	20.6918	2170.2682	0.010	0.992
factor(alpha)8	21.0027	2170.2682	0.010	0.992
factor(alpha)9	-0.8226	3182.4092	0.000	1.000
factor(alpha)10	17.6670	2170.2683	0.008	0.994
factor(alpha)11	17.9902	2170.2682	0.008	0.993
factor(alpha)12	18.9552	2170.2682	0.009	0.993
factor(alpha)13	21.7355	2170.2682	0.010	0.992
factor(alpha)14	20.7316	2170.2682	0.010	0.992
factor(alpha)15	19.9737	2170.2682	0.009	0.993
factor(alpha)16	20.3374	2170.2682	0.009	0.993
factor(class)1:factor(surv)0	-0.8577	0.1573	-5.451	5.00e-08 ***
factor(class)2:factor(surv)0	0.1604	0.1738	0.923	0.356
factor(class)3:factor(surv)0	0.9201	0.1486	6.192	5.93e-10 ***
factor(class)1:factor(surv)1	NA	NA	NA	NA
factor(class)2:factor(surv)1	NA	NA	NA	NA
factor(class)3:factor(surv)1	NA	NA	NA	NA
factor(age)1:factor(surv)0	1.0615	0.2440	4.350	1.36e-05 ***
factor(age)1:factor(surv)1	NA	NA	NA	NA
factor(sex)1:factor(surv)0	2.4201	0.1404	17.236	< 2e-16 ***
factor(sex)1:factor(surv)1	NA	NA	NA	NA

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 4953.14 on 31 degrees of freedom
Residual deviance: 112.57 on 10 degrees of freedom
AIC: 283.97

Number of Fisher Scoring iterations: 15

The variable `alpha` is added to correspond to the α_i terms from (2). Consider the gender effect in specific. Here, 2.42 suggests the odds of surviving for a male were roughly 9% that of a female. Furthermore, the estimate is highly significant. To calculate an exact P-value for this problem we use `simulateConditional` to simulate tables conditioning on all of the parameters except the one corresponding to the `factor(surv) : factor(sex)` interaction.

```
> chain <- simulateConditional(y ~ factor(surv) +
+                             (factor(class) + factor(age)) : factor(surv) +
+                             factor(alpha),
+                             dat = titanic.dat,
+                             nosim = 10 ^ 3,
+                             method = "cab",
+                             p = .1)
```

A P-value for a score test of $H_0 : \gamma = 0$ versus $H_a : \gamma < 0$ simply counts the proportion of tables with sufficient statistic for γ is smaller than the observed value. Using the notation from (2) the sufficient statistic for γ is $s_\gamma = \sum_i z_i y_i \equiv z'y$. We calculate the chain of sufficient statistics and the observed sufficient statistic below.

```
> z <- titanic.dat$sex * titanic.dat$surv
> sgamma <- chain %*% z
> sgamma.obs <- titanic.dat$y %*% z
> mean(sgamma <= sgamma.obs[1])
```

```
[1] 0.032
```

Apparently, none of the simulated tables have sufficient statistics for γ below that of the observed, which agrees closely with large sample results above.

5 Discussion and To Do

In this manual we investigated three straightforward examples of `exactLoglinTest` and considered two useful extensions of the program. The program was initially constructed calculate P-values for goodness of fit tests for contingency tables. However, the latter examples suggest a more user friendly interface for those problems would be useful.

Finally, it should be noted that only the inner-most calculations have been migrated to C. Possibly great gains in the speed of the algorithm could be attained by migrating more of the code (or more efficient R coding).

References

- [1] Alan Agresti. *Categorical Data Analysis*. Wiley, New York, 1990.
- [2] J.G. Booth and R.W. Butler. An importance sampling algorithm for exact conditional test in log-linear models. *Biometrika*, 86:321–332, 1999.
- [3] Brian S. Caffo and James G. Booth. A markov chain monte carlo algorithm for approximating exact conditional probabilities. *the Journal of Computational and Graphical Statistics*, 10:730–745, 2001.
- [4] Adrian Dobra, Claudia Tebaldi, and Mike West. Reconstruction of contingency tables with missing data. Technical report, Duke University, 2002.
- [5] D. E. Edwards and T. Havranek. A fast procedure for model search in multidimensional contingency tables. *Biometrika*, 72:339–351, 1985.
- [6] Friedrich Leisch. *Sweave User Manual*.
- [7] W. N. Venables and B. D. Ripley. *Modern Applied Statistics with S*. Springer, New York, fourth edition, 2002.

A Tables

Residence in 1980	Residence in 1985			
	Northeast	Midwest	South	West
Northeast	11,607	100	366	124
Midwest	87	13,677	515	302
South	172	225	17,819	270
West	63	176	286	10,192

Source [1]

Table 1: Residency Data

Pathologist A	Pathologist B				
	1	2	3	4	5
1	22	2	2	0	0
2	5	7	14	0	0
3	0	2	36	0	0
4	0	1	14	7	0
5	0	0	3	0	3

Source [1]

Table 2: Pathologist Agreement Data

Lake	Gender	Size	Primary Food Choice				
			Fish	Invert	Reptile	Bird	Other
1	Male	Small	7	1	0	0	5
	Male	Large	4	0	0	1	2
	Female	Small	16	3	2	2	3
	Female	Large	3	0	1	2	3
2	Male	Small	2	2	0	0	1
	Male	Large	13	7	6	0	0
	Female	Small	3	9	1	0	2
	Female	Large	0	1	0	1	0
3	Male	Small	3	7	1	0	1
	Male	Large	8	6	6	3	5
	Female	Small	2	4	1	1	4
	Female	Large	0	1	0	0	0
4	Male	Small	13	10	0	2	2
	Male	Large	9	0	0	1	2
	Female	Small	3	9	1	0	1
	Female	Large	8	1	0	0	1

Source [1]

Model (FG, FL, FS, LGS) where F=food choice, L=lake, S=size, G=gender.

Table 3: Alligator Data

F	E	D	C	B					
				A	no		yes		
				no	yes	no	yes		
neg	small	small	no	44	40	112	67		
			yes	129	145	12	23		
		large	no	35	12	80	33		
			yes	109	67	7	9		
	large	small	no	23	32	70	66		
			yes	50	80	7	13		
		large	no	24	25	73	57		
			yes	51	63	7	16		
			pos	small	no	5	7	21	9
					yes	9	17	1	4
large	no	4			3	11	8		
	yes	14			17	5	2		
large	small	no		7	3	14	14		
		yes		9	16	2	3		
	large	no		4	0	13	11		
		yes		5	14	4	4		

Source [4] originally appeared in [5].

Table 4: Czech Auto Workers Data

Surv	Sex	Age	Class			
			Crew	First	Second	Third
no	F	Child	0	0	0	17
		Adult	3	4	13	89
	M	Child	0	0	0	35
		Adult	670	118	154	387
yes	F	Child	0	1	13	14
		Adult	20	140	80	76
	M	Child	0	5	11	13
		Adult	192	57	14	75